

# Finite-State Technology in Natural Language Processing

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# Roadmap

- 1 Linguistic Basics and Weighted Automata
- 2 Part-of-Speech Tagging
- 3 Parsing
- 4 Machine Translation

Always ask questions right away!

## Units

- **Sentence** (syntactic unit expressing complete thought)
  - ▶ Alla sätt är bra utom de dåliga.
  - ▶ “Are you serious?” she asked.

## Units

- Sentence (syntactic unit expressing complete thought)
- Clause (grammatically complete syntactic unit)
  - ▶ Vännens örfil är ärligt menad, fiendens kyssar vill bedra.  
(2 main clauses)
  - ▶ People who live in glass houses should not throw stones.  
(main clause + relative clause)

## Units

- Sentence (syntactic unit expressing complete thought)
- Clause (grammatically complete syntactic unit)
- **Phrases** (smaller syntactic units)
  - ▶ **the green car** (noun phrase = noun and its modifiers)
  - ▶ **killed the snake** (verb phrase = verb and its objects)

## Units

- Sentence (syntactic unit expressing complete thought)
- Clause (grammatically complete syntactic unit)
- Phrases (smaller syntactic units)
- **Token** (smallest unit = “word”; often derived from lexicon entry)
  - ▶ house, car, lived, smallest, 45th, STACS, Knuth
  - ▶ but tricky: Knuth's vs. Knuth 's; well-known vs. well - known

## Tokenization

Splitting text into sentences and tokens

- relatively simple for English, Swedish, German, etc.  
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Example (English sentence-ending full stop)

RE `. <WhiteSpace>+ [A-Z]` covers most cases (in English)

## Example (English)

- tokens usually separated by whitespace
- sentence end marker “.” highly ambiguous:
  - ▶ common abbreviations
  - ▶ dates, ordinals, and phone numbers

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- sentence end marker “.” highly ambiguous:
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  - ▶ dates, ordinals, and phone numbers
- **STANFORD** tokenizer
  - ▶ implemented in **JAVA**
  - ▶ compiles RegEx into DFA and runs DFA
  - ▶ can process 1,000,000 tokens per second

(based on JFlex)

# Weighted Automata

## Definition

A **weighted automaton** is a system  $(Q, \Sigma, I, \Delta, F, wt)$

- finite set  $Q$  of states
- input alphabet  $\Sigma$
- initial states  $I \subseteq Q$
- transitions  $\Delta \subseteq Q \times \Sigma \times Q$
- final states  $F \subseteq Q$

## Example



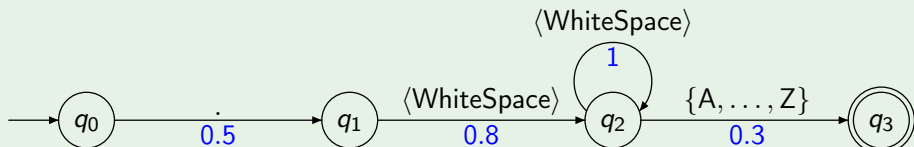
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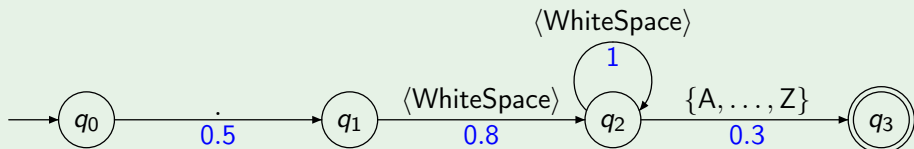
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## Example



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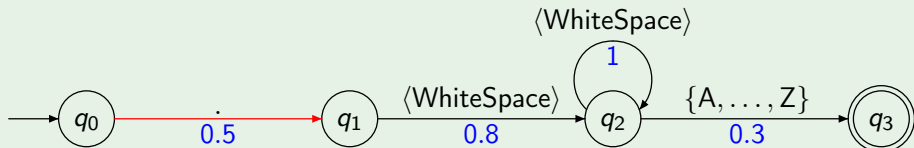
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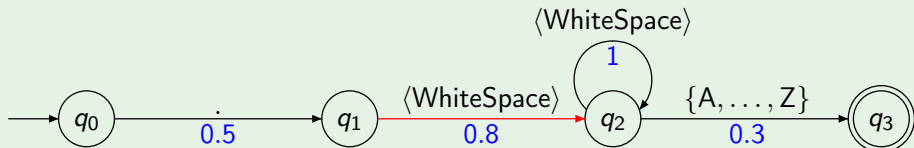


## Definition (Semantics)

- **Weight of a run:** product of the transition weights  
(run  $(q_0, \cdot, q_1)(q_1, \langle \text{WhiteSpace} \rangle, q_2)(q_2, F, q_3)$  has weight  $0.5 \cdot 0.8 \cdot 0.3 = 0.12$ )

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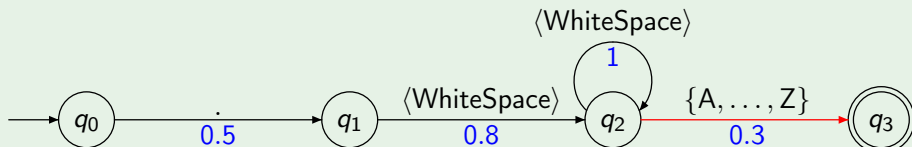


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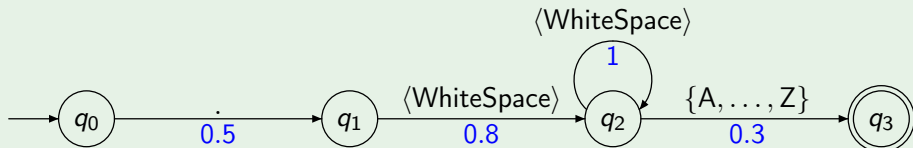


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- **Weight of an input:** sum of the weights of all successful runs  
(input  $\cdot \_ F$  has weight 0.12)

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DT NN

# Part-of-Speech Tagging

## History

- 1960s

- ▶ manually tagged BROWN corpus (1,000,000 words)
- ▶ tag lists with frequency for each token  
e.g., {VB, MD, NN} for can
- ▶ excluding ling.-implausible sequences (e.g. DT VB)
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### ● 2000s

- ▶ British national corpus (100,000,000 words)
- ▶ parsers are better taggers (wTA algorithms)

## Statistical approach

Given a sequence  $w = w_1 \cdots w_k$  of tokens,  
determine the most likely sequence  $t_1 \cdots t_k$  of part-of-speech tags  
( $t_i$  is the tag of  $w_i$ )

$$\begin{aligned}(\hat{t}_1, \dots, \hat{t}_k) &= \arg \max_{(t_1, \dots, t_k)} p(t_1, \dots, t_k \mid w) \\ &= \arg \max_{(t_1, \dots, t_k)} \frac{p(t_1, \dots, t_k, w)}{p(w)} \\ &= \arg \max_{(t_1, \dots, t_k)} p(t_1, \dots, t_k, w_1, \dots, w_k) \\ &= \arg \max_{(t_1, \dots, t_k)} p(t_1, w_1) \cdot \prod_{i=2}^k p(t_i, w_i \mid t_1, \dots, t_{i-1}, w_1, \dots, w_{i-1})\end{aligned}$$

## Modelling as stochastic process

- introduce event  $E_i = w_i \cap t_i = (w_i, t_i)$

$$\begin{aligned} & p(t_1, w_1) \cdot \prod_{i=2}^k p(t_i, w_i \mid t_1, \dots, t_{i-1}, w_1, \dots, w_{i-1}) \\ &= p(E_1) \cdot \prod_{i=2}^k p(E_i \mid E_1, \dots, E_{i-1}) \end{aligned}$$

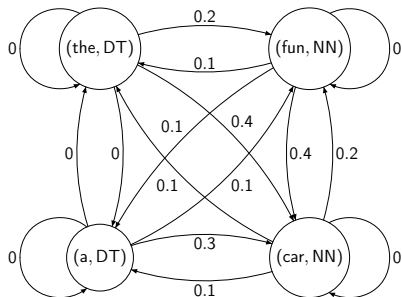
- assume **MARKOV** property

$$p(E_i \mid E_1, \dots, E_{i-1}) = p(E_i \mid E_{i-1}) = p(E_2 \mid E_1)$$

# Markov Model

## Summary

- initial weights  $p(E)$  (not indicated below)
- transition weights  $p(E | E')$



## Maximum likelihood estimation (MLE)

Assume that likelihood = relative frequency in corpus

- initial weights  $p(E)$   
How often does  $E$  start a tagged sentence?
- transition weights  $p(E | E')$   
How often does  $E$  follow  $E'$ ?

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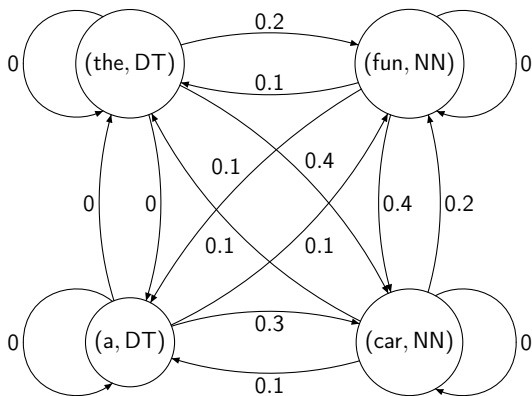
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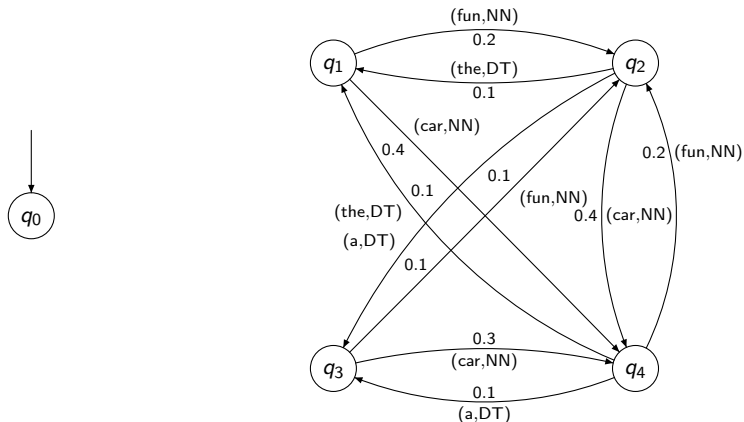
## Problems

- **Vocabulary:**  $\approx$  350,000 English tokens, but only 50,000 tokens (14%) in **BROWN** corpus
- **Sparsity:** (**car**, **NN**) (**fun**, **NN**) not attested in corpus, but plausible (frequency estimates might be wrong)

# Transformation into Weighted Automaton

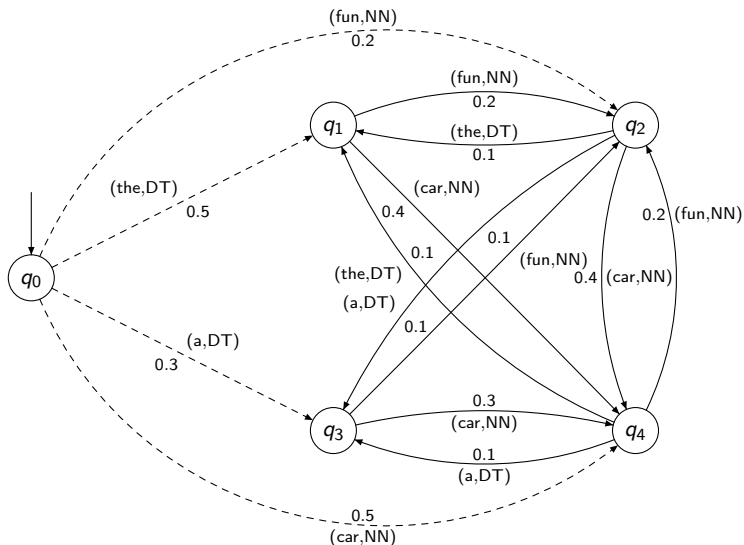


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## Typical questions

- **Decoding:** (or language model evaluation)  
Given model  $M$  and sentence  $w$ , determine probability  $M_1(w)$ 
  - ▶ project labels to first components
  - ▶ evaluate  $w$  in the obtained wA  $M_1$
  - ▶ **efficient:** initial-algebra semantics (forward algorithm)

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  - ▶ **efficient:** initial-algebra semantics (forward algorithm)
- **Tagging:**  
Given model  $M$  and sentence  $w$ ,  
determine the best tag sequence  $t_1 \cdots t_k$ 
  - ▶ intersect  $M$  with the DFA for  $w$  and any tag sequence
  - ▶ determine best run in the obtained wA
  - ▶ **efficient:** VITERBI algorithm

## Typical questions

- **(Weight) Induction:** (or MLE training)  
Given NFA  $(Q, \Sigma, I, \Delta, F)$  and sequence  $\bar{w}_1, \dots, \bar{w}_k$  of **tagged** sentences  $\bar{w}_i \in \Sigma^*$ , determine transition weights **wt**:  $\Delta \rightarrow [0, 1]$  such that  $\prod_{i=1}^k M_{\text{wt}}(\bar{w}_i)$  is maximal with  $M_{\text{wt}} = (Q, \Sigma, I, \Delta, F, \text{wt})$ 
  - ▶ no closed solution (in general), but many approximations
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- **Learning:** (or HMM induction)  
Given NFA  $(Q, \Sigma, I, \Delta, F)$  and sequence  $w_1, \dots, w_k$  of **untagged** sentences  $w_i$ , determine transition weights **wt**:  $\Delta \rightarrow [0, 1]$  such that  $\prod_{i=1}^k (M_{\text{wt}})_1(w_i)$  is maximal with  $M_{\text{wt}} = (Q, \Sigma, I, \Delta, F, \text{wt})$ 
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## Issues

- **WA too big** (in comparison to training data)
    - ▶ cannot reliably estimate that many probabilities  $p(E | E')$
    - ▶ simplify model
- e.g., assume transition probability only depends on tags

$$p((w, t) | (w', t')) = p(t | t')$$

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- **unknown words**
  - ▶ no statistics on words that do not occur in corpus
  - ▶ allow only assignment of **open** tags  
(open tag = potentially unbounded number of elements, e.g. NNP)  
(closed tag = fixed finite number of elements, e.g. DT or PRP)
  - ▶ use morphological clues (capitalization, affixes, etc.)
  - ▶ use context to disambiguate
  - ▶ use “global” statistics

## TCS contributions

- **efficient evaluation and complexity considerations**  
(initial-algebra semantics, best runs, best strings, etc.)
- **model simplifications**  
(trimming, determinization, minimization, etc.)
- **model transformations**  
(projection, intersection, RegEx-to-DFA, etc.)
- **model induction**  
(grammar induction, weight training, etc.)



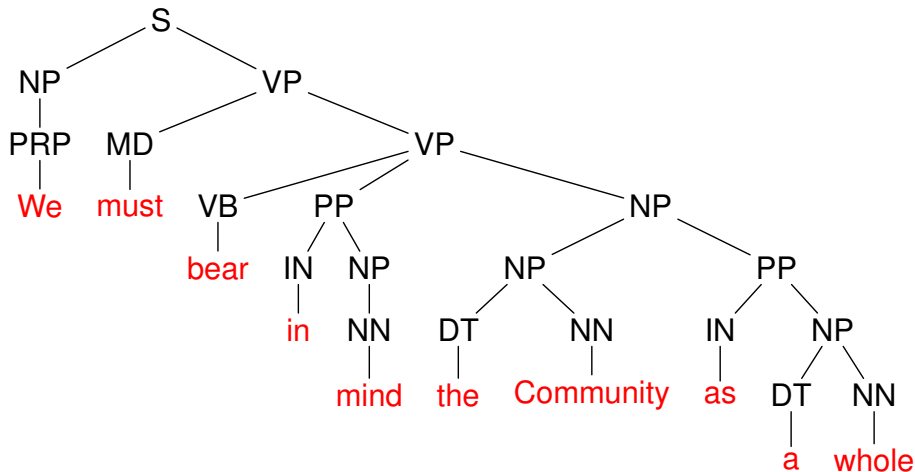
# Parsing

## Motivation

- **(syntactic) parsing**  
= determining the syntactic structure of a sentence
- important in several applications:
  - ▶ co-reference resolution  
(determining which noun phrases refer to the same object/concept)
  - ▶ comprehension  
(determining the meaning)
  - ▶ speech repair and sentence-like unit detection in speech  
(speech offers no punctuation; needs to be predicted)

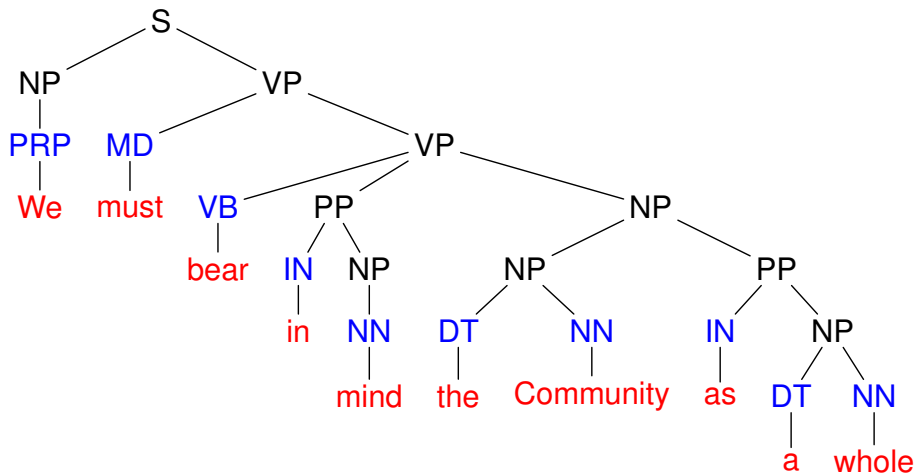
# Parsing

We must bear in mind the Community as a whole



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# Trees

Finite sets  $\Sigma$  and  $W$

## Definition

Set  $T_\Sigma(W)$  of  $\Sigma$ -trees indexed by  $W$  is smallest  $T$

- $w \in T$  for all  $w \in W$
- $\sigma(t_1, \dots, t_k) \in T$  for all  $k \in \mathbb{N}$ ,  $\sigma \in \Sigma$ , and  $t_1, \dots, t_k \in T$

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## Notes

- obvious recursion & induction principle

## Problem

- assume a hidden  $g: W^* \rightarrow T_\Sigma(W)$  (reference parser)
- given a finite set  $T \subseteq T_\Sigma(W)$  (training set)  
generated by  $g$
- develop a system representing  $f: W^* \rightarrow T_\Sigma(W)$  (parser)  
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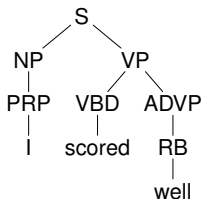
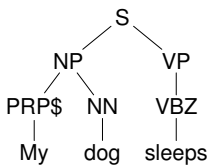
## Clarification

- $T$  generated by  $g \iff T = g(L)$  for some finite  $L \subseteq W^*$
- for approximation we could use  $|\{w \in W^* \mid f(w) = g(w)\}|$

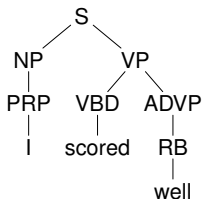
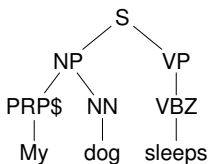
## Short history

- **before 1990**
  - ▶ hand-crafted rules based on POS tags (unlexicalized parsing)
  - ▶ corrections and selection by human annotators
- **1990s**
  - ▶ **PENN** tree bank (1,000,000 words)
  - ▶ weighted local tree grammars (weighted CFG) as parsers (often still unlexicalized)
  - ▶ **WALL STREET JOURNAL** tree bank (30,000,000 words)
- **since 2000**
  - ▶ weighted tree automata (weighted CFG with latent variables)
  - ▶ lexicalized parsers

# Weighted Local Tree Grammars



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## LTG production extraction

simply read off CFG productions:

$S \rightarrow NP VP$	$NP \rightarrow PRP\$ NN$
$PRP\$ \rightarrow My$	$NN \rightarrow dog$
$VP \rightarrow VBZ$	$VBZ \rightarrow sleeps$
$NP \rightarrow PRP$	$PRP \rightarrow I$
$VP \rightarrow VBD ADVP$	$VBD \rightarrow scored$
$ADVP \rightarrow RB$	$RB \rightarrow well$

## Observations

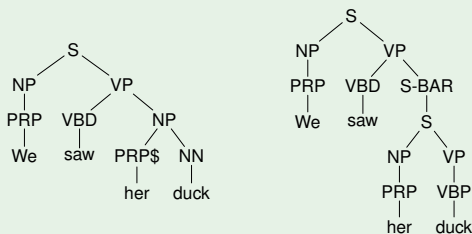
- LTG offer unique explanation on tree level  
(rules observable in training data; as for POS tagging)
  - but ambiguity on the string level  
(i.e., on unannotated data; as for POS tagging)
- weighted productions

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## Observations

- LTG offer unique explanation on tree level  
(rules observable in training data; as for POS tagging)
  - but ambiguity on the string level  
(i.e., on unannotated data; as for POS tagging)
- weighted productions

## Illustration



# Weighted Local Tree Grammars

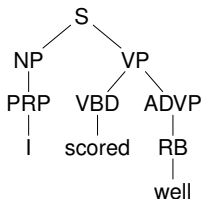
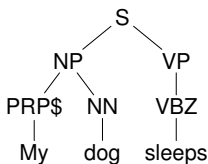
## Definition

A **weighted local tree grammar** (wLTG) is a weighted CFG  $G = (N, W, S, P, wt)$

- finite set  $N$  (nonterminals)
- finite set  $W$  (terminals)
- $S \subseteq N$  (start nonterminals)
- finite set  $P \subseteq N \times (N \cup W)^*$  (productions)
- mapping  $wt: P \rightarrow [0, 1]$  (weight assignment)

It computes the weighted derivation trees of the wCFG

# Weighted Local Tree Grammars



## wLTG production extraction

simply read of CFG productions and keep counts:

$S \rightarrow NP VP$ (2)	$NP \rightarrow PRP\$ NN$ (1)
$PRP\$ \rightarrow My$ (1)	$NN \rightarrow dog$ (1)
$VP \rightarrow VBZ$ (1)	$VBZ \rightarrow sleeps$ (1)
$NP \rightarrow PRP$ (1)	$PRP \rightarrow I$ (1)
$VP \rightarrow VBD ADVP$ (1)	$VBD \rightarrow scored$ (1)
$ADVP \rightarrow RB$ (1)	$RB \rightarrow well$ (1)



# Weighted Local Tree Grammars

## wLTG production extraction

normalize counts:

(here by left-hand side)

S  $\rightarrow$  NP VP (2)

NP  $\rightarrow$  PRP\$ NN (1)

NP  $\rightarrow$  PRP (1)

PRP\$  $\rightarrow$  My (1)

NN  $\rightarrow$  dog (1)

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# Weighted Local Tree Grammars

## wLTG production extraction

normalize counts:

(here by left-hand side)

$S \xrightarrow{1} NP VP$

$NP \xrightarrow{0.5} PRP\$ NN$

$NP \xrightarrow{0.5} PRP$

$PRP\$ \xrightarrow{1} My$

$NN \xrightarrow{1} dog$

$VP \xrightarrow{0.5} VBZ$

$VP \xrightarrow{0.5} VBD ADVP$

$VBZ \xrightarrow{1} sleeps$

$PRP \xrightarrow{1} I$

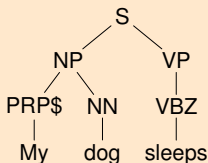
$VBD \xrightarrow{1} scored$

$ADVP \xrightarrow{1} RB$

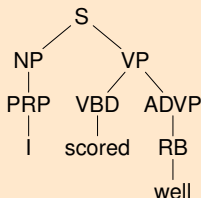
$RB \xrightarrow{1} well$

# Weighted Local Tree Grammars

## Weighted parses



weight: 0.25



weight: 0.25

## Weighted LTG productions

(only productions with weight  $\neq 1$ )

$\text{NP} \xrightarrow{0.5} \text{PRP\$ NN}$

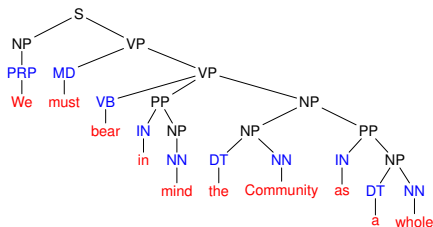
$\text{VP} \xrightarrow{0.5} \text{VBZ}$

$\text{NP} \xrightarrow{0.5} \text{PRP}$

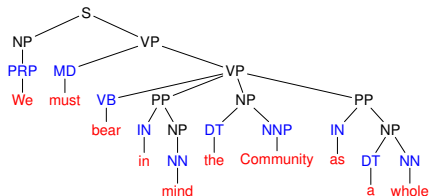
$\text{VP} \xrightarrow{0.5} \text{VBD ADVP}$

# Parser Evaluation

BERKELEY parser [Reference]:



CHARNIAK-JOHNSON parser:



## Definition (ParseEval measure)

- **precision** = number of correct constituents  
(heading the same phrase as in reference)  
divided by number of all constituents in parse

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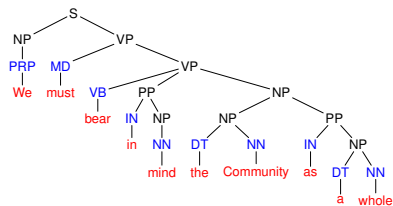
## Definition (ParseEval measure)

- **precision** = number of correct constituents (heading the same phrase as in reference) divided by number of all constituents in parse
- **recall** = number of correct constituents divided by number of all constituents in reference
- (weighted) harmonic mean

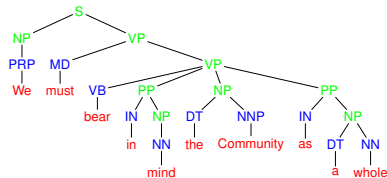
$$F_{\alpha} = (1 + \alpha^2) \cdot \frac{\text{precision} \cdot \text{recall}}{\alpha^2 \cdot \text{precision} + \text{recall}}$$

# Parser Evaluation

## Reference



## Parser output

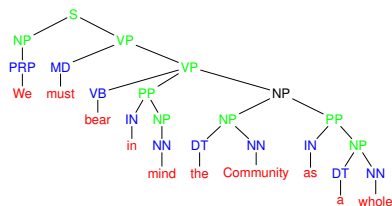


● precision =  $\frac{9}{9} = 100\%$

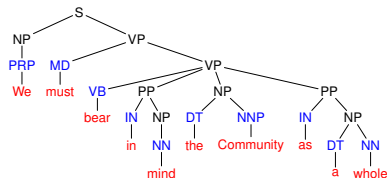


# Parser Evaluation

## Reference



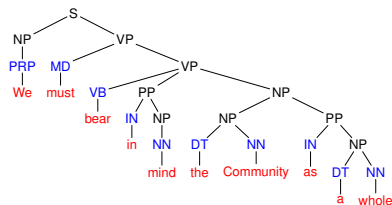
## Parser output



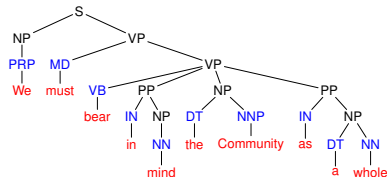
- **precision** =  $\frac{9}{9} = 100\%$
- **recall** =  $\frac{9}{10} = 90\%$

# Parser Evaluation

## Reference



## Parser output



- **precision** =  $\frac{9}{9} = 100\%$
- **recall** =  $\frac{9}{10} = 90\%$
- **$F_1$**  =  $2 \cdot \frac{1 \cdot 0.9}{1 + 0.9} = 95\%$

## Standardized Setup

- **training data:** PENN treebank Sections 2–21  
(articles from the WALL STREET JOURNAL)
- **development test data:** PENN treebank Section 22
- **evaluation data:** PENN treebank Section 23

## Experiment [POST, GILDEA, '09]

grammar model	precision	recall	$F_1$
wLTG	75.37	70.05	72.61

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grammar model	precision	recall	$F_1$
wLTG	75.37	70.05	72.61

These are bad compared to the state-of-the-art!

## State-of-the-art models

- **context-free grammars with latent variables** ( $\text{CFG}_{\text{lv}}$ )  
[COLLINS, '99], [KLEIN, MANNING, '03], [PETROV, KLEIN, '07]
- **tree substitution grammars with latent variables** ( $\text{TSG}_{\text{lv}}$ )  
[SHINDO et al., '12]
- (both as expressive as weighted tree automata)
- other models

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[SHINDO et al., '12]
- (both as expressive as weighted tree automata)
- other models

## Experiment [SHINDO et al., '12]

grammar model	$F_1$
wLTG = wCFG	72.6
wTSG [COHN et al., 2010]	84.7
wCFG <sub>lv</sub> [PETROV, 2010]	91.8
wTSG <sub>lv</sub> [SHINDO et al., 2012]	92.4

## Definition

A **grammar with latent variables** is (grammar with relabeling)

- a grammar  $G$  generating  $L(G) \subseteq T_{\Sigma}(W)$
- a (total) mapping  $\rho: \Sigma \rightarrow \Delta$  **functional relabeling**

# Grammars with Latent Variables

## Definition

A **grammar with latent variables** is (grammar with relabeling)

- a grammar  $G$  generating  $L(G) \subseteq T_{\Sigma}(W)$
- a (total) mapping  $\rho: \Sigma \rightarrow \Delta$  **functional relabeling**

## Definition (Semantics)

$$L(G, \rho) = \rho(L(G)) = \{\rho(t) \mid t \in L(G)\}$$

Language class: **REL**( $\mathcal{L}$ ) for language class  $\mathcal{L}$



# Weighted Tree Automata

## Definition

A **weighted tree automaton** (wTA) is a system  $G = (Q, N, W, S, P, wt)$

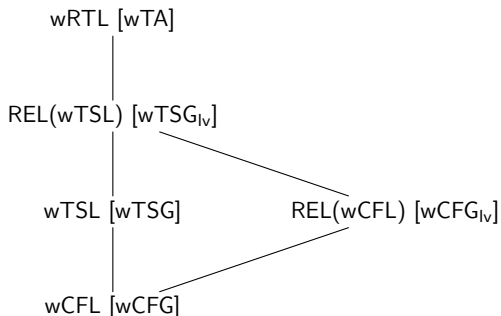
- **finite set  $Q$**  (states)
- finite set  $N$  (nonterminals)
- finite set  $W$  (terminals)
- $S \subseteq Q$  (start states)
- finite set  $P \subseteq (Q \times N \times (Q \cup W)^+) \cup (Q \times W)$  (productions)
- mapping  $wt: P \rightarrow [0, 1]$  (weight assignment)

production  $(q, n, w_1, \dots, w_k)$  is often written  $q \rightarrow n(w_1, \dots, w_k)$

# Grammars with Latent Variables

## Theorem

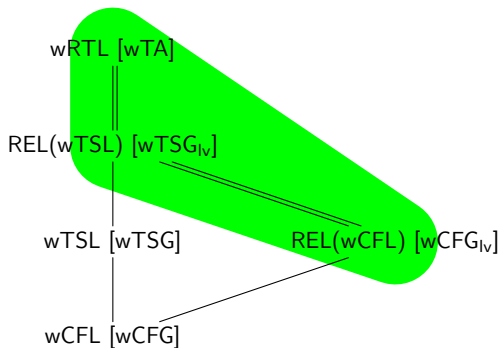
$$\text{REL}(w\text{LTL}) = \text{REL}(w\text{TSL}) = w\text{RTL}$$



# Grammars with Latent Variables

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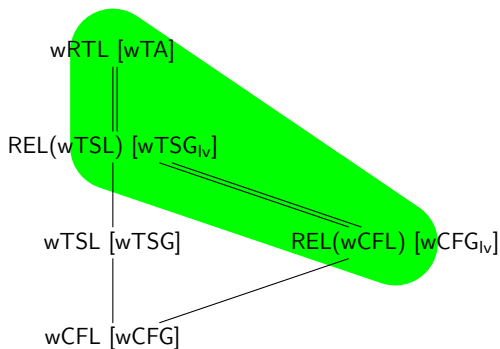
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# Grammars with Latent Variables

## Theorem

$$\text{REL}(w\text{LTL}) = \text{REL}(w\text{TSL}) = w\text{RTL}$$



here: **latent variables**  $\approx$  **finite-state**

## Typical questions

- **Decoding:** (or language model evaluation)  
Given model  $M$  and sentence  $w$ , determine probability  $M(w)$ 
  - ▶ intersect  $M$  with the DTA for  $w$  and any parse
  - ▶ evaluate  $w$  in the obtained WTA
  - ▶ **efficient:** initial-algebra semantics (forward algorithm)

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  - ▶ evaluate  $w$  in the obtained WTA
  - ▶ **efficient:** initial-algebra semantics (forward algorithm)
- **Parsing:**  
Given model  $M$  and sentence  $w$ , determine the best parse  $t$  for  $w$ 
  - ▶ intersect  $M$  with the DTA for  $w$  and any parse
  - ▶ determine best **tree** in the obtained WTA
  - ▶ **efficient:** none (NP-hard even for wLTG)

## Statistical parsing approach

Given wLTG  $M$  and sentence  $w$ , return highest-scoring parse for  $w$

# Parsing

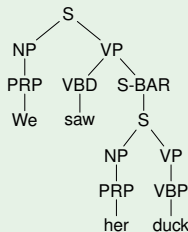
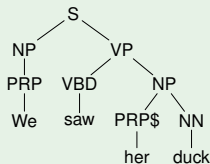
## Statistical parsing approach

Given wLTG  $M$  and sentence  $w$ , return highest-scoring parse for  $w$

## Consequence

The first parse should be preferred

(“duck” more frequently a noun, etc.)





## TCS contributions

- **efficient evaluation and complexity considerations**  
(initial-algebra semantics, best runs, best trees, etc.)
- **model simplifications**  
(trimming, determinization, minimization, etc.)
- **model transformations**  
(intersection, normalization, lexicalization, etc.)
- **model induction**  
(grammar induction, weight training, spectral learning, etc.)

## NLP contribution to TCS

- good source of (relevant) problems
- good source for practical techniques (e.g., fine-to-coarse decoding)
- good source of (relevant) large wTA

<b>language</b>	<b>states</b>	<b>non-lexical productions</b>
English	1,132	1,842,218
Chinese	994	1,109,500
German	981	616,776

# Machine Translation

## Applications

- Technical manuals

## Example (An mp3 player)

The synchronous manifestation of lyrics is a procedure for can broadcasting the music, waiting the mp3 file at the same time showing the lyrics.

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The synchronous manifestation of lyrics is a procedure for can broadcasting the music, waiting the mp3 file at the same time showing the lyrics. With the this kind method that the equipments that synchronous function of support up broadcast to make use of document create setup, you can pass the LCD window way the check at the document contents that broadcast. That procedure returns offerings to have to modify, and delete, and stick top , keep etc. edit function.

## Applications

- Technical manuals
- US military

## Example (Speech-to-text [JONES et al., '09])

*E:* Okay, what is your name?

*A:* Abdul.

*E:* And your last name?

*A:* Al Farran.

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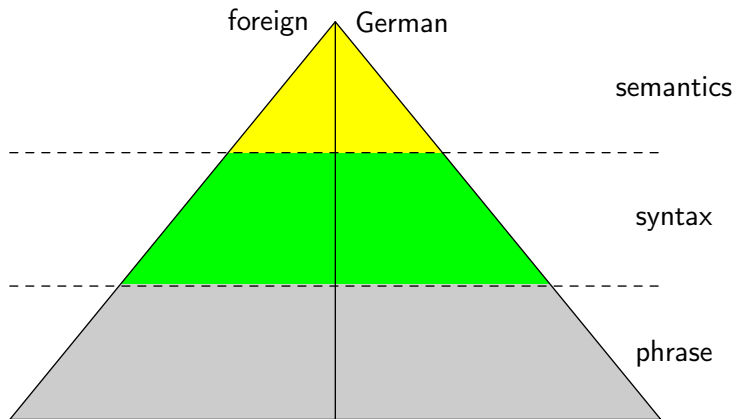
*A:* milk a mechanic and I am here  
I mean yes

*E:* What is your last name?

*A:* every two weeks  
my son's name is ismail

# Machine Translation

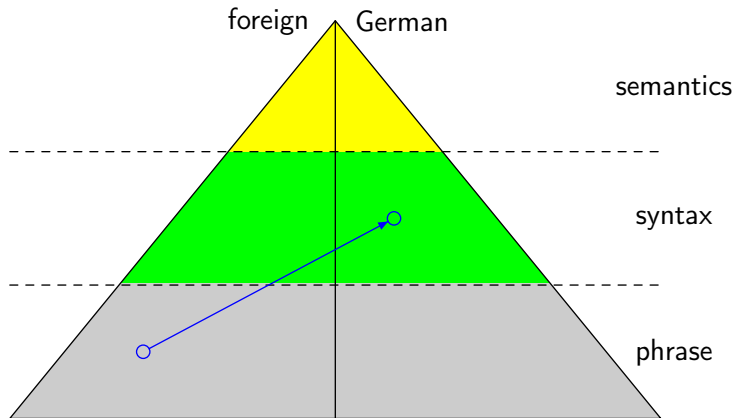
VAUQUOIS triangle:



Translation model:

# Machine Translation

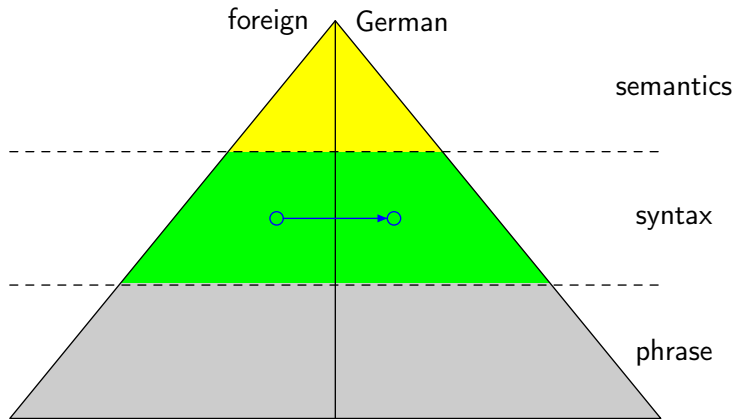
VAUQUOIS triangle:



Translation model: [string-to-tree](#)

# Machine Translation

VAUQUOIS triangle:



Translation model: [tree-to-tree](#)

## Training data

- parallel corpus
- word alignments
- parse trees for the target sentences

# Machine Translation

## Training data

- parallel corpus
- word alignments
- parse trees for the target sentences

## Parallel Corpus

linguistic resource containing example translations

(sentence level)

# Machine Translation

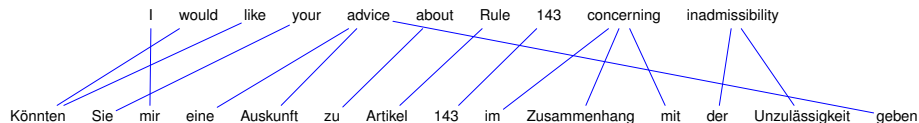
parallel corpus, word alignments, parse tree

I would like your advice about Rule 143 concerning inadmissibility

Könnten Sie mir eine Auskunft zu Artikel 143 im Zusammenhang mit der Unzulässigkeit geben

# Machine Translation

parallel corpus, **word alignments**, parse tree

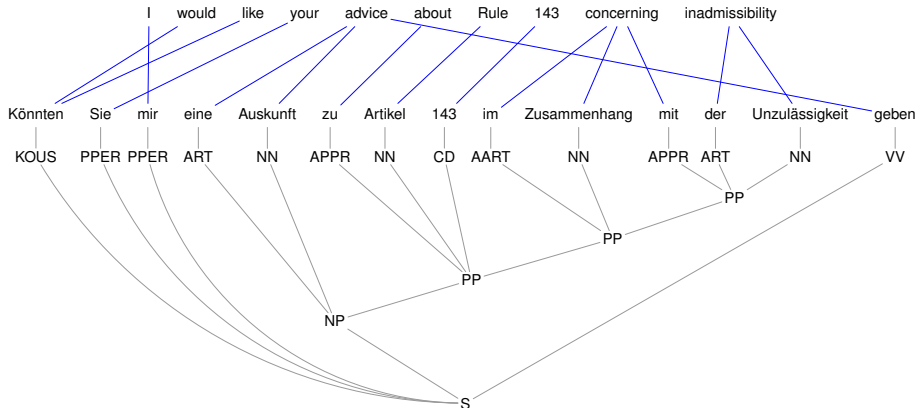


via GIZA++ [OCH, NEY, '03]



# Machine Translation

parallel corpus, word alignments, **parse tree**



via BERKELEY parser [PETROV et al., '06]

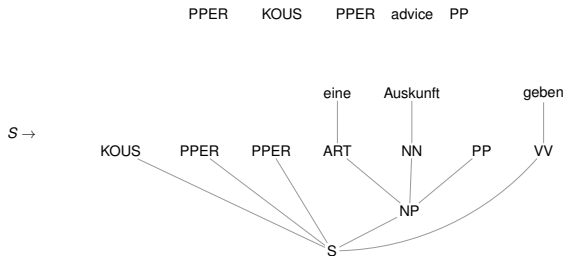
## Extended top-down tree transducer (STSG)

- variant of [M., GRAEHL, HOPKINS, KNIGHT, '09]
- rules of the form  $NT \rightarrow (r, r_1)$  for nonterminal  $NT$ 
  - ▶ right-hand side  $r$  of context-free grammar rule
  - ▶ right-hand side  $r_1$  of regular tree grammar rule

# Extended Tree Transducer

## Extended top-down tree transducer (STSG)

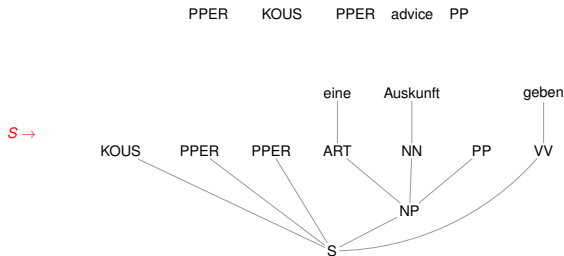
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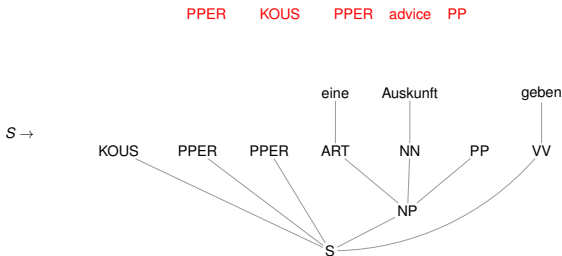
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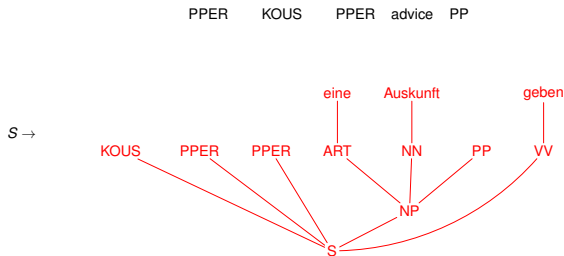
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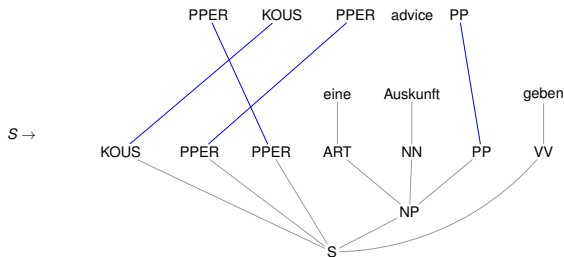
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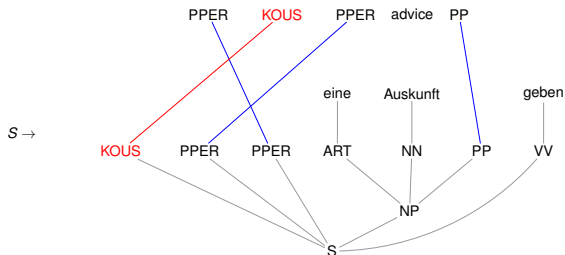
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  - ▶ right-hand side  $r$  of context-free grammar rule
  - ▶ right-hand side  $r_1$  of regular tree grammar rule
- (bijective) synchronization of nonterminals







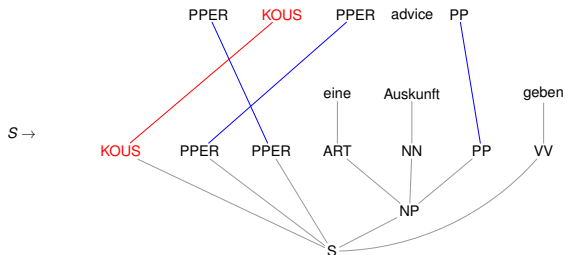
# Extended Tree Transducer



## Rule application

- 1 Selection of synchronous nonterminals

# Extended Tree Transducer



## Rule application

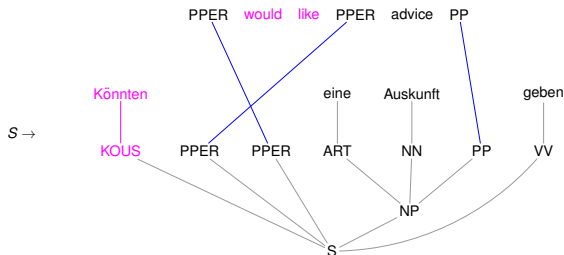
- 1 Selection of synchronous nonterminals
- 2 Selection of suitable rule

KOUS →

would like

Könnten  
|  
KOUS

# Extended Tree Transducer



## Rule application

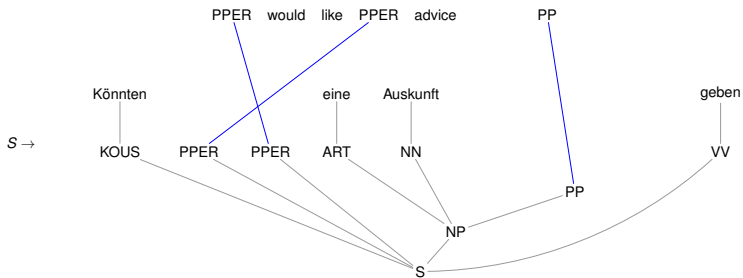
- 1 Selection of synchronous nonterminals
- 2 Selection of suitable rule
- 3 Replacement on both sides

KOUS →

would like

Könnten  
|  
KOUS

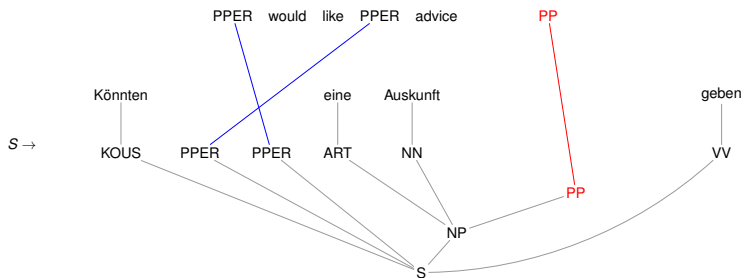
# Extended Tree Transducer



## Rule application

- 1 synchronous nonterminals

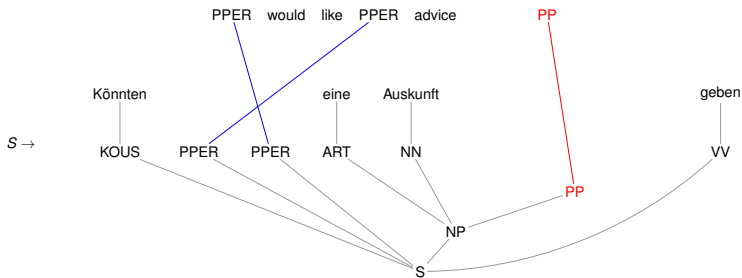
# Extended Tree Transducer



## Rule application

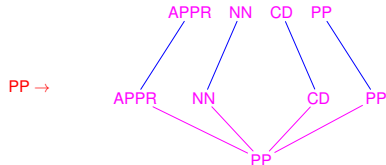
- 1 synchronous nonterminals

# Extended Tree Transducer

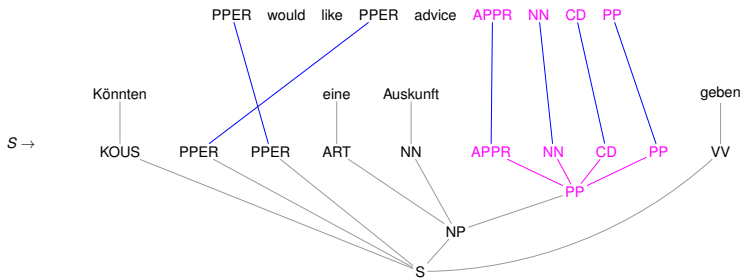


## Rule application

- 1 synchronous nonterminals
- 2 suitable rule

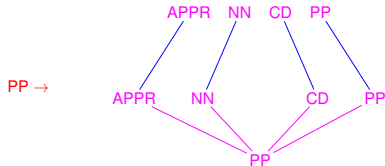


# Extended Tree Transducer



## Rule application

- 1 synchronous nonterminals
- 2 suitable rule
- 3 replacement



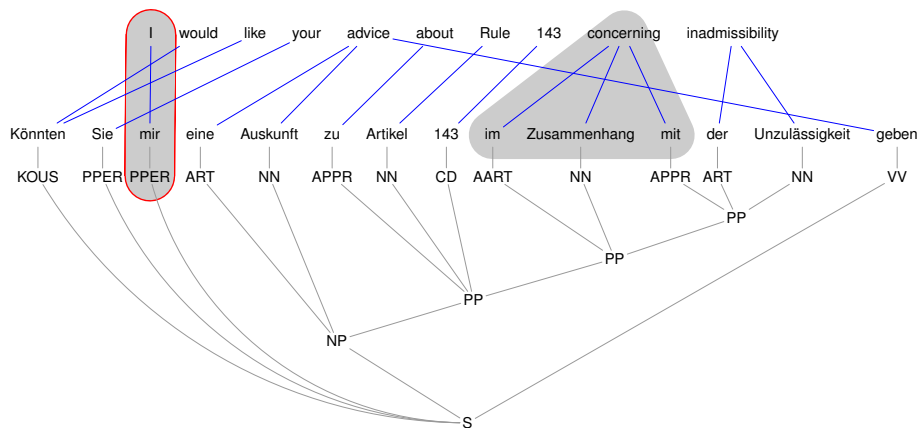






# Rule extraction

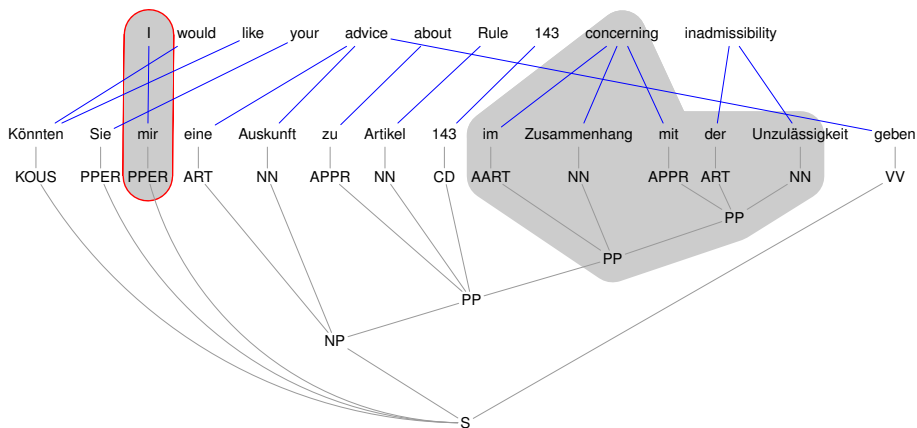
following [GALLEY, HOPKINS, KNIGHT, MARCU, '04]



extractable rules marked in red

# Rule extraction

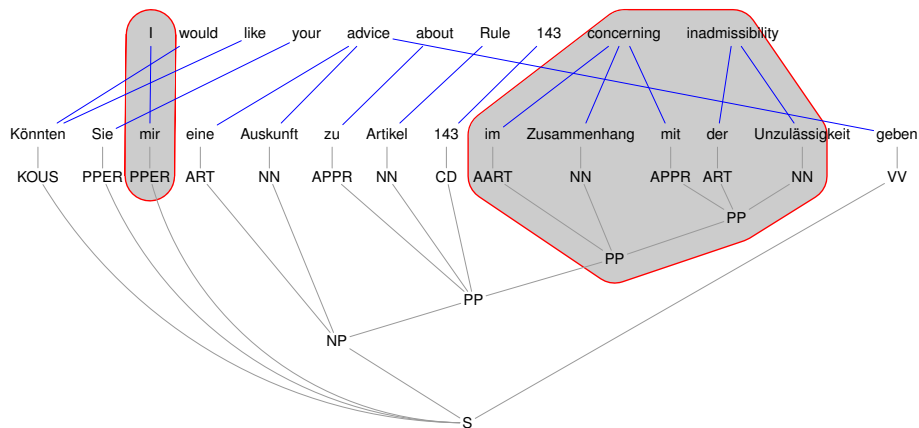
following [GALLEY, HOPKINS, KNIGHT, MARCU, '04]



extractable rules marked in red

# Rule extraction

following [GALLEY, HOPKINS, KNIGHT, MARCU, '04]

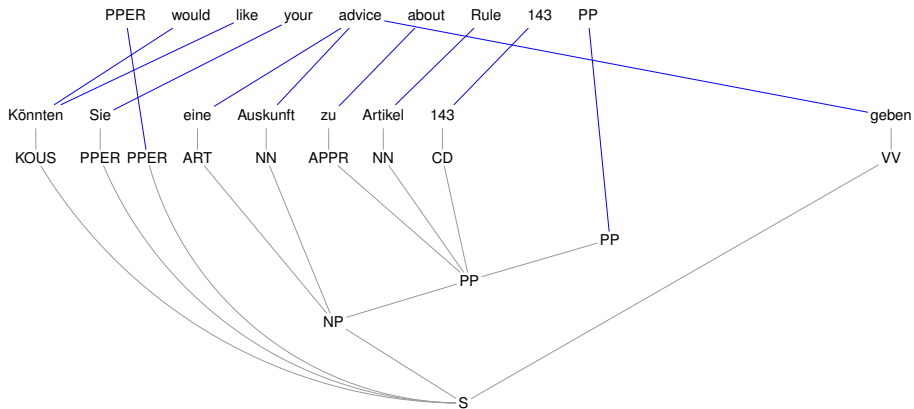


extractable rules marked in red



# Rule extraction

## Removal of extractable rule:



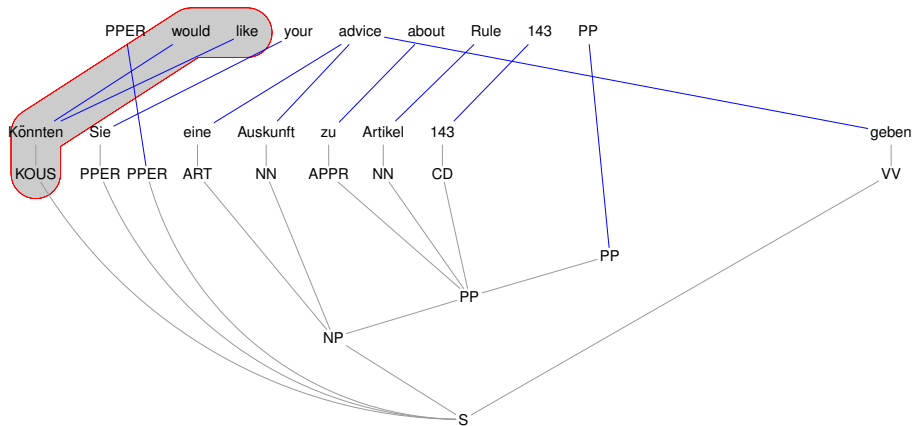






# Rule extraction

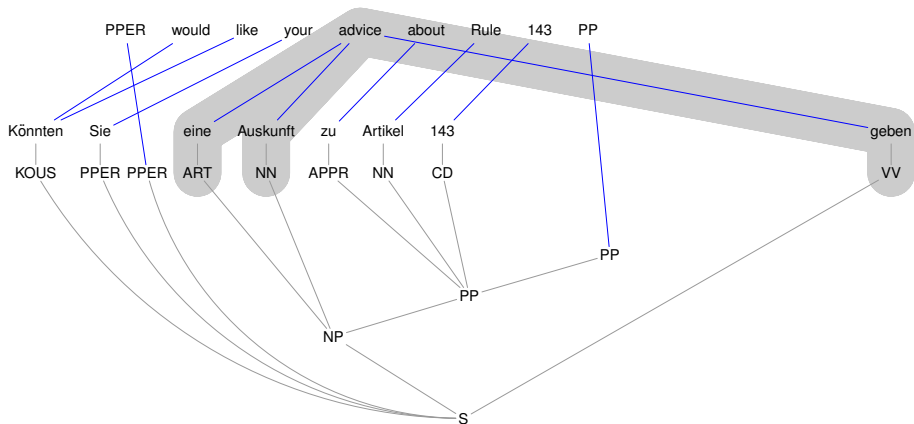
Repeated rule extraction:



extractable rules marked in red

# Rule extraction

Repeated rule extraction:

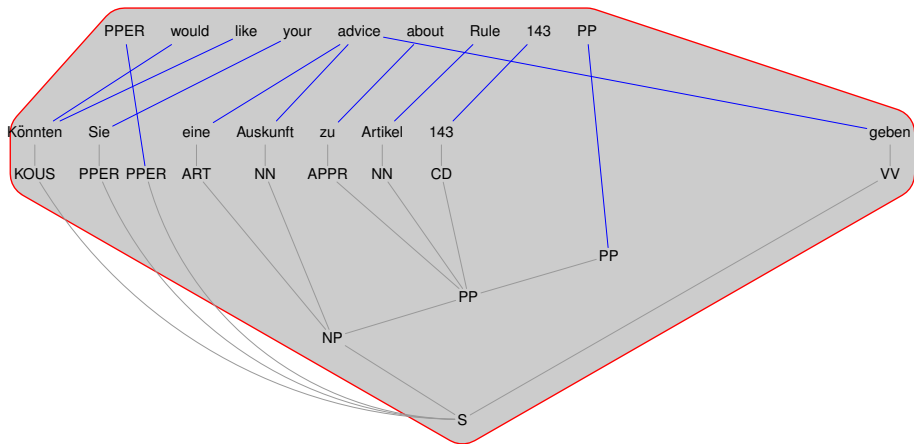


extractable rules marked in red



# Rule extraction

Repeated rule extraction:



extractable rules marked in red

## Advantages

- very simple
- implemented in MOSES [KOEHN et al., '07]
- “context-free”

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## Disadvantages

- problems with discontinuities
- composition and binarization not possible [M. et al., '09] and [ZHANG et al., '06]
- “context-free”

## Remarks

- synchronization breaks almost all existing constructions (e.g., the normalization construction)
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- the basic grammar model **very important**
- **tree-to-tree** models use trees on both sides



## Major (tree-to-tree) models

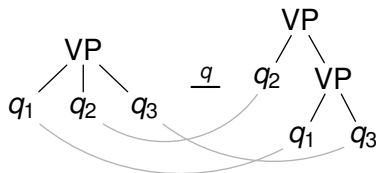
- ① **linear top-down tree transducer (with look-ahead)**
  - ▶ input-side: **tree automaton**
  - ▶ output-side: **regular tree grammar**
  - ▶ synchronization: **mapping output NT to input NT**

## Major (tree-to-tree) models

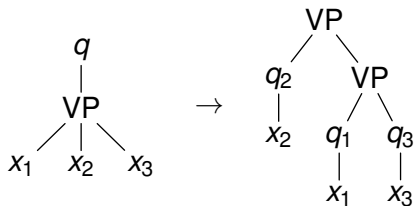
- 1 **linear top-down tree transducer (with look-ahead)**
  - ▶ input-side: tree automaton
  - ▶ output-side: regular tree grammar
  - ▶ synchronization: mapping output NT to input NT
- 2 **linear extended top-down tree transducer (w. look-ahead)**
  - ▶ input-side: regular tree grammar
  - ▶ output-side: regular tree grammar
  - ▶ synchronization: mapping output NT to input NT

# Extended Tree Transducer

Synchronous grammar rule:



“Classical” top-down tree transducer rule:



## Syntactic restrictions

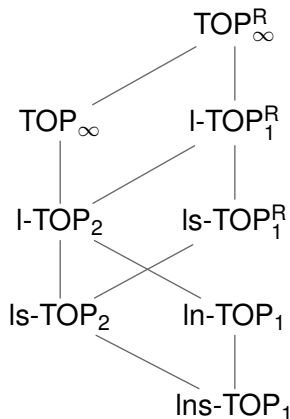
- nondeleting if synchronization bijective (in all rules)
- strict if  $r_1$  not a nonterminal (for all rules  $q \rightarrow (r, r_1)$ )
- $\epsilon$ -free if  $r$  not a nonterminal (for all rules  $q \rightarrow (r, r_1)$ )

## Composition (COMP)

executing transformations  $\tau \subseteq T_\Sigma \times T_\Delta$  and  $\tau' \subseteq T_\Delta \times T_\Gamma$   
one after the other:

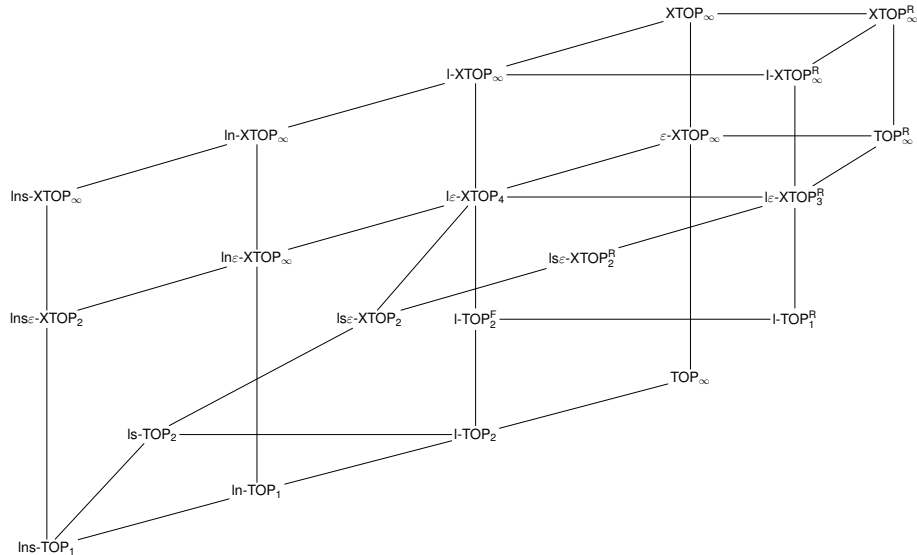
$$\tau ; \tau' = \{(s, u) \mid \exists t \in T_\Delta : (s, t) \in \tau, (t, u) \in \tau'\}$$

# Top-down Tree Transducer



composition closure indicated in subscript

# Extended Tree Transducer



composition closure indicated in subscript

## TCS contributions

- **efficient evaluation and complexity considerations**  
(exact decoding, best runs, best translations, etc.)
- **evaluation of expressive power**  
(which linguistic phenomena can be captured?  
relationship to other models)
- **model transformations**  
(intersection, language model integration,  
parse forest decoding, etc.)
- **very little on model induction so far**  
(mostly local models so far; power of finite-state not yet explored)







# Evaluation

<b>Task</b>	<b>System</b>	<b>BLEU</b>
English → German	STSG	15.22
	MBOT	15.90
	phrase-based	16.73
	hierarchical	16.95
	GHKM	17.10
English → Arabic	STSG	48.32
	MBOT	49.10
	phrase-based	50.27
	hierarchical	51.71
	GHKM	46.66
English → Chinese	STSG	17.69
	MBOT	18.35
	phrase-based	18.09
	hierarchical	18.49
	GHKM	18.12

from [SEEMANN et al., '15]



# Selected Literature

-  **ENGELFRIET**: *Bottom-up and Top-down Tree Transformations — A Comparison*. Math. Systems Theory 9 '75
-  **KLEIN, MANNING**: *Accurate Unlexicalized Parsing*  
Proc. ACL '03
-  **KOEHN**: *Statistical Machine Translation*  
Cambridge University Press '10
-  **MANNING, SCHÜTZE**: *Foundations of Statistical Natural Language Processing*. MIT Press '99
-  **PETROV, BARRETT, THIBAU AND KLEIN**: *Learning Accurate, Compact, and Interpretable Tree Annotation*. Proc. ACL '06
-  **SHINDO, MIYAO, FUJINO AND NAGATA**: *Bayesian Symbol-Refined Tree Substitution Grammars for Syntactic Parsing*. Proc. ACL '12