

How to train your multi bottom-up tree transducer

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Portland, OR — June 22, 2011



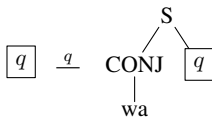
Synchronous Tree Substitution Grammar

q

q

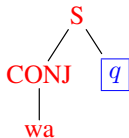
Used rule

Next rule

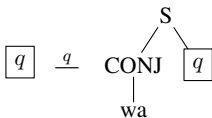


Synchronous Tree Substitution Grammar

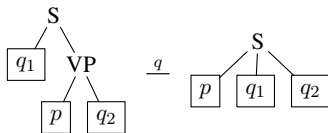
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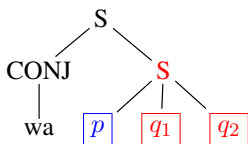
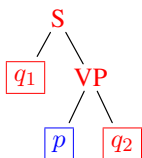
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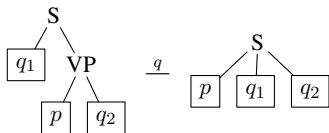
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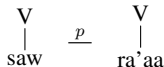
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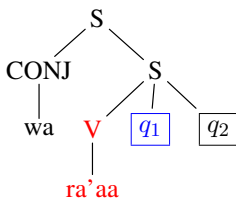
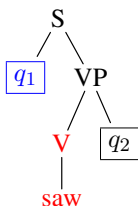
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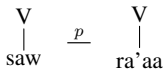
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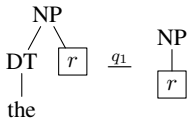
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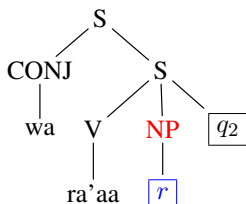
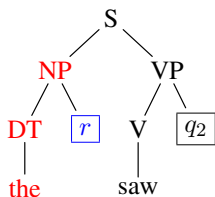
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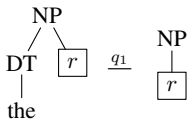
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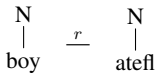
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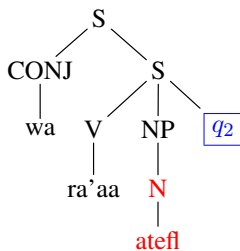
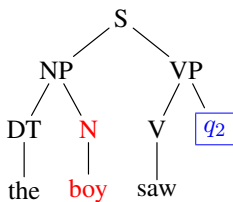
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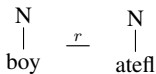
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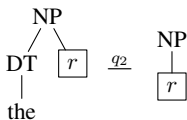
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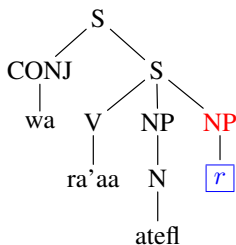
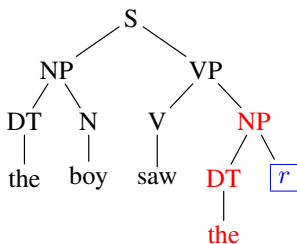
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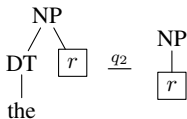
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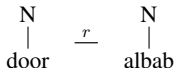
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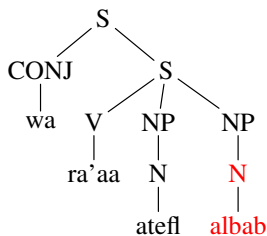
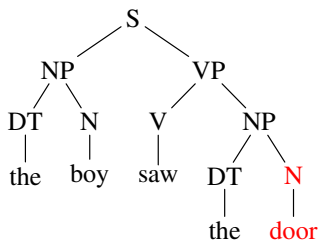
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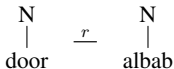
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Synchronous Tree Substitution Grammar



Used rule



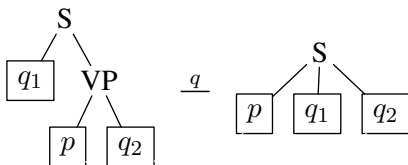
Next rule



Synchronous Tree Substitution Grammar

Rule shape

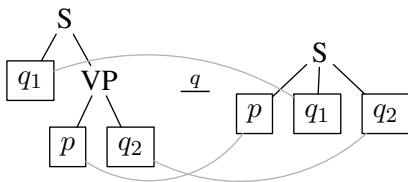
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 - states in rhs = states in lhs
 - exactly one lhs and one rhs
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Notes

- version with states (instead of locality tests)
- equivalent to linear nondeleting extended tree transducers
- implemented in TIBURON [[May, Knight 2006](#)]



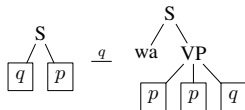
Multi Bottom-up Tree Transducer

q

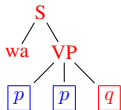
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Used rule

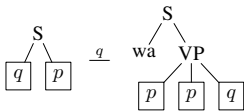
Next rule



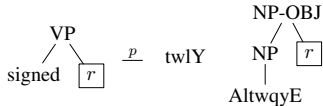
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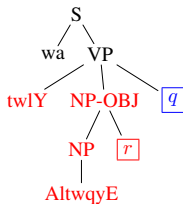
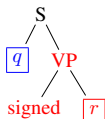
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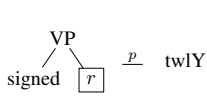
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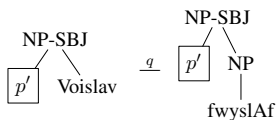
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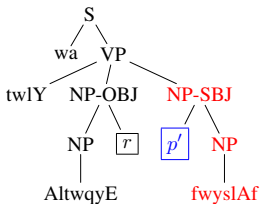
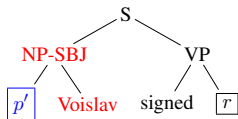
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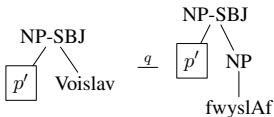
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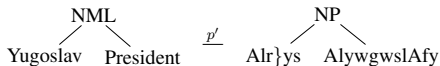
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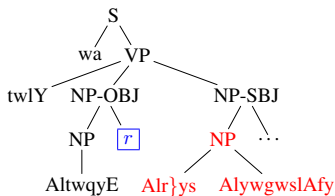
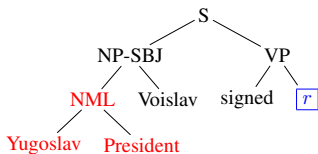
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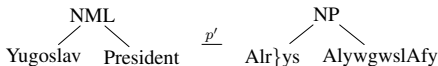
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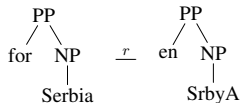
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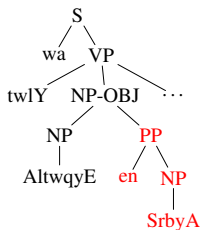
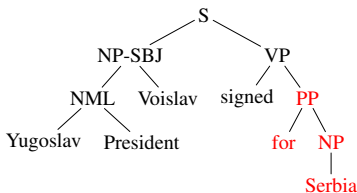
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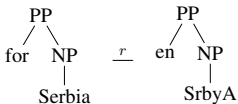
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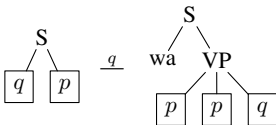
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Multi Bottom-up Tree Transducer

Rule shape

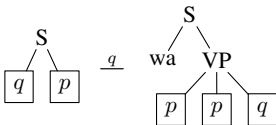
- STSG: states can occur only once in lhs and rhs
MBOT: states can occur only once in lhs
 - STSG: states in rhs = states in lhs
MBOT: states in rhs \subseteq states in lhs
 - STSG: exactly one lhs and one rhs
MBOT: exactly one lhs
- STSG: bijective synchronization relation
MBOT: inverse synchronization relation is functional



Multi Bottom-up Tree Transducer

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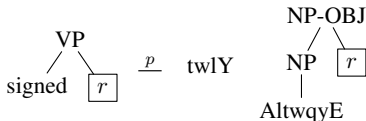
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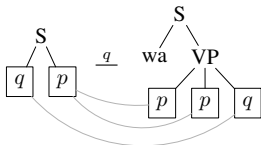
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STSG vs. MBOT

property	STSG	MBOT
simple and natural	✓	?
symmetric	✓	✗
preserves regularity	✓	✗
inverse pres. regularity	✓	✓
binarizable	✗	✓
closed under composition	✗	✓
input parsing	$\mathcal{O}(M n^x)$	$\mathcal{O}(M n^3)$
output parsing	$\mathcal{O}(M n^x)$	$\mathcal{O}(M n^y)$

where $x = 2 \operatorname{rk}(M) + 5$ and
 $y = 2 \operatorname{rk}(M) + 2$



Additional Expressive Power

Finite copying

$$\{\langle t, \sigma(t, t) \rangle \mid t \in \mathcal{T}_\Sigma\}$$

- ✓ desirable [ATANLP participants, 2010]
e.g., for cross-serial dependencies
- ✗ harms preservation of regularity

Non-contiguous rules

- ✓ +0.64 BLEU [Sun, Zhang, Tan, 2009] 25.92 → 26.56
- ✓ do not harm preservation of regularity



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Approach

Old approach

- 1 extract STSG rules
- 2 train STSG
- 3 convert to MBOT
- 4 work with MBOT

New approach

- 1 extract (restricted) MBOT rules
- 2 train MBOT
- 3 work with MBOT



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Roadmap

- 1 Motivation
- 2 Relation to STSSG
- 3 Rule Extraction and Training
- 4 Preservation of Recognizability



Synchronous Tree-Sequence Substitution Grammar

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- STSG: states can occur only once in lhs and rhs
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Expressive Power

Corollary

$$\text{STSG} \subseteq \text{MBOT} \subseteq \text{STSSG}$$

Theorem

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Claim

$$\text{MBOT}^{-1} ; \text{MBOT} = \text{STSSG}$$



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Rule Extraction

Input

- parallel bi-text
- parses for input and output
- word alignment

Output

- MBOT rules



Rule Extraction

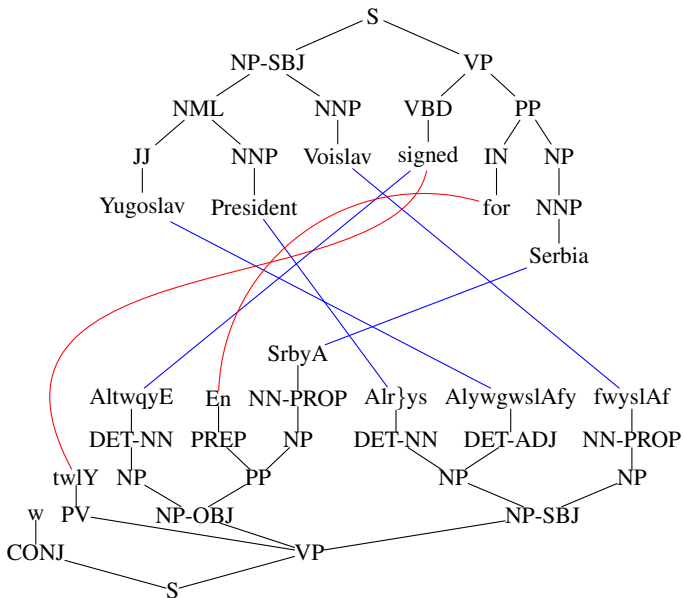
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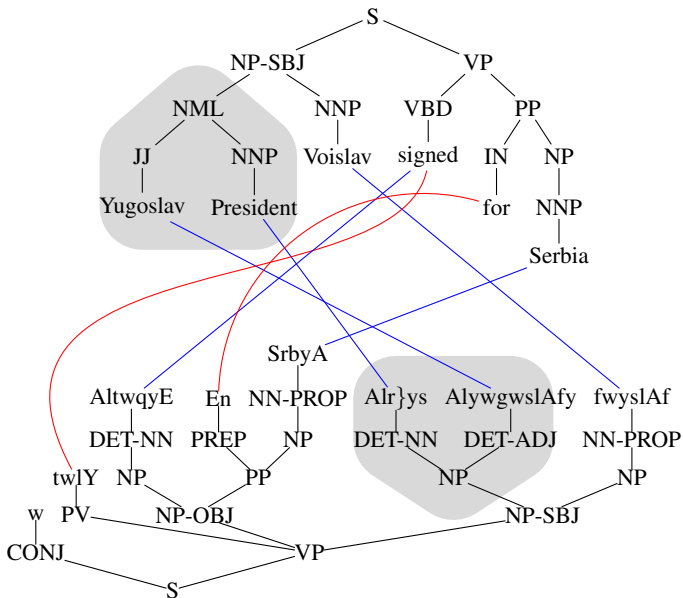
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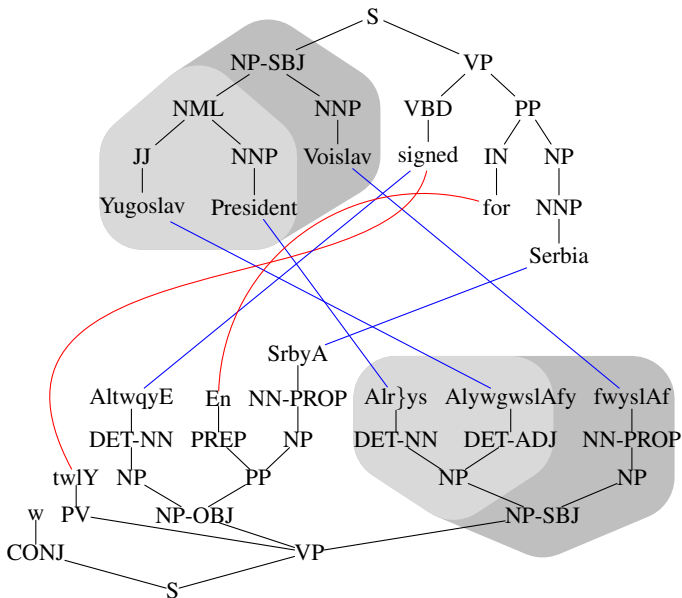
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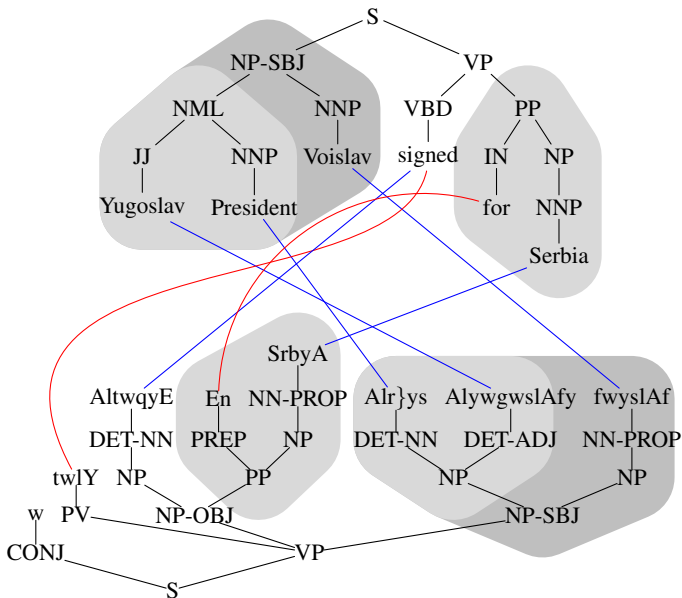
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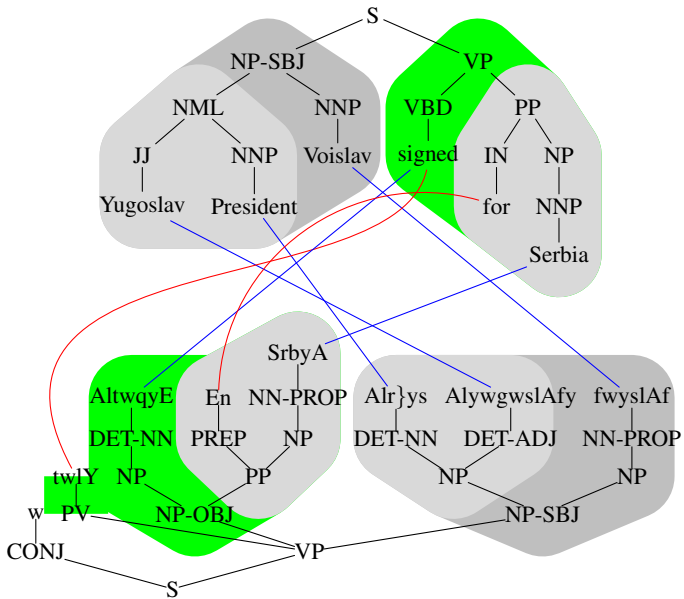




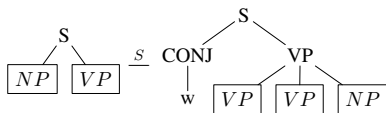
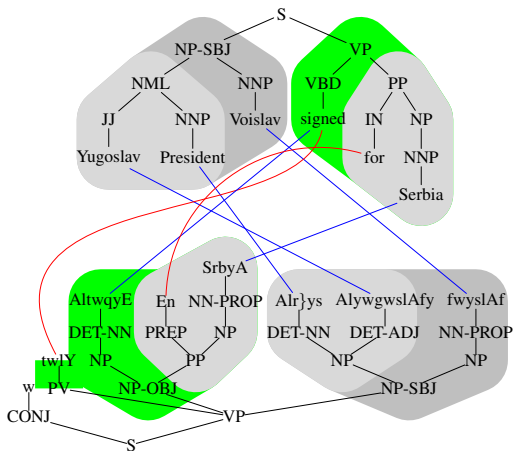




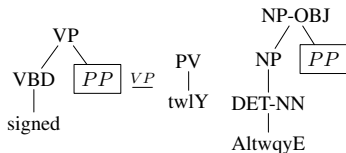
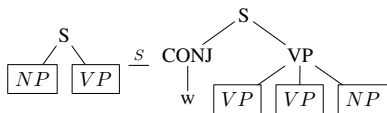
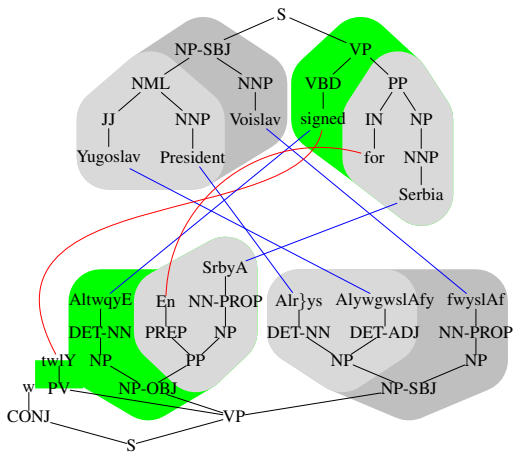




Rule Extraction



Rule Extraction

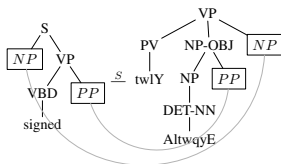


Extracted Rules

STSG rule

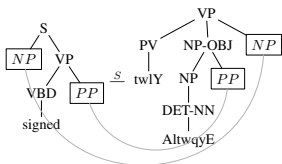
MBOT rules

STSSG rule

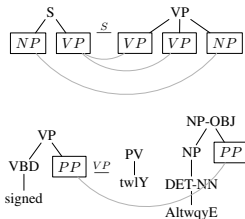


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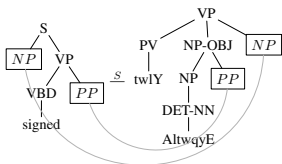
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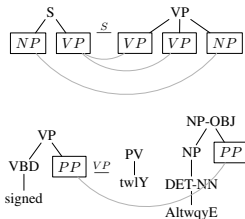
STSSG rule

Extracted Rules

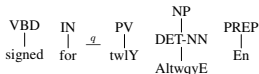
STSG rule



MBOT rules



STSSG rule



Definition

A tree language is **regular** if it can be represented by a TSG (with states).

Example

$$\{\sigma(t, t) \mid t \in T_{\Sigma}\}$$

is **not** regular.



Theorem

The set of derivations of an MBOT is regular.

Conclusion

Minimal adaptation of [Graehl, Knight, May 2008] can be used.



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Roadmap

- 1 Motivation
- 2 Relation to STSSG
- 3 Rule Extraction and Training
- 4 Preservation of Recognizability



Preservation of Regularity

Input

- MBOT M
- regular tree language L

Question

Is $M(L) = \{t \mid \exists s \in L: \langle s, t \rangle \in M\}$ regular?

Example

- $M = \{\langle t, \sigma(t, t) \rangle \mid t \in \mathcal{T}_\Sigma\}$
- infinite, but regular tree language $L \subseteq \mathcal{T}_\Sigma$

Then $M(L) = \{\sigma(t, t) \mid t \in L\}$ is **not** regular.



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Preservation of Regularity

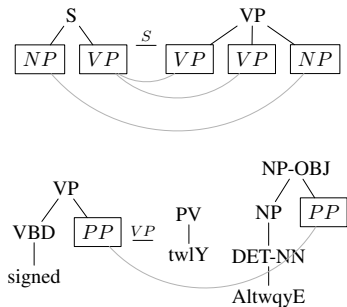
Why desired?

- easy and efficient representation of output languages
- allows intersection with (regular) language model
- allows bucket-brigade algorithms
[[May, Knight, Vogler, 2010](#)]

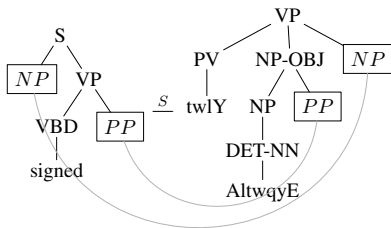


Rule Composition

Input rules



Output rule



Rule Composition

Power MBOT

$$M^k = \{R_1 \circ \dots \circ R_k \mid R_1, \dots, R_k \in M\}$$

Explanation

- M^k contains k -fold composed rules
- composition fails if states do not match
- composition succeeds (with no effect) if no matchable states present



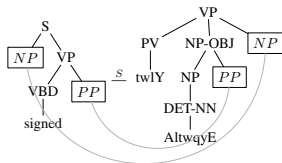
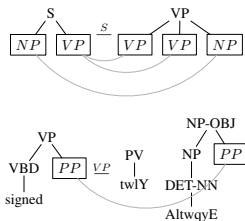
Finitely Collapsing

Definition

M is **finitely collapsing** if there exists $k \in \mathbb{N}$ such that

- every state occurs at most once in rhs of every rule of M^k .

Example



Finite Synchronization

Definition

M has **finite synchronization** if there exists $k \in \mathbb{N}$ such that

- all occurrences of a state occur in the same tree in the rhs of every rule of M^k .

Theorem (Raoult, 1997)

MBOT with finite synchronization and finitely collapsing MBOT preserve regularity.



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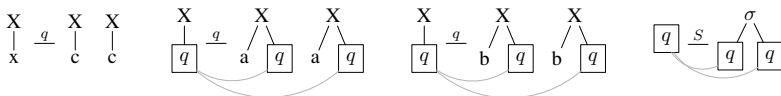
Copy-free

Definition

M is **copy-free** if there exists $k \in \mathbb{N}$ such that for every rule of M^k and all occurrences w of a state:

- w is the root of a tree in the rhs or
- w belongs to a fixed tree in the rhs.

Example (not copy-free)



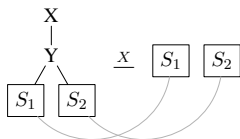
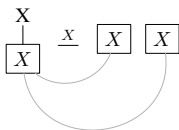
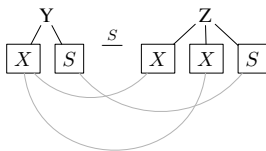
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Example (copy-free)



Main Result

Theorem

Copy-free MBOT preserve regularity.

Theorem

finitely collapsing \subset finite synchronization \subset copy-free

Note

All 3 restrictions can be guaranteed during rule extraction.



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Thank you for your attention!



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