## A Gentle Introduction to Weighted Extended Top-down Tree Transducers

#### Andreas Maletti

Universitat Rovira i Virgili Tarragona, Spain

email: andreas.maletti@urv.cat

#### Leipzig — May 3, 2010



Weighted Extended Top-down Tree Transducers

## Collaborators

#### Joint work with

- JOOST ENGELFRIET, LIACS, Leiden, The Netherlands
- ZOLTÁN FÜLÖP, University of Szeged, Hungary
- JONATHAN GRAEHL, USC, LOS Angeles, CA, USA
- MARK HOPKINS, Language Weaver Inc., Los Angeles, CA, USA
- KEVIN KNIGHT, USC, Los Angeles, CA, USA
- ERIC LILIN, Université de Lille, France
- HEIKO VOGLER, TU Dresden, Germany





## Weighted Extended Top-down Tree Transducer









# Motivation

## Example (Input in Catalan)

Benvolguda i benvolgut membre de la comunitat universitària, Avui dilluns es duu a terme el darrer Consell de Govern del meu mandat com a rector; el proper dia 6 de maig, com correspon, hi haurà una nova elecció on tota la comunitat universitària podrà escollir nou rector o rectora. Aquest darrer consell té, naturalment, un caràcter marcadament tècnic; l'ordre del dia complet el trobaràs adjunt al final d'aquest text. A continuació et comento només els punts que, al meu parer, poden ser més del teu interès.

#### Translation (GOOGLE TRANSLATE) to English

Dear and beloved member of the university community, Today is Monday carried out by the Governing Council last of my term as rector, the next day, May 6, as appropriate, there will be another election where the entire university community can choose new rector. This last advice is, of course, a markedly technician complete agenda can be found attached to the end of this text. Then I said only the points that I believe may be of interest.



# Motivation

#### Example (Input in Catalan)

Benvolguda i benvolgut membre de la comunitat universitària, Avui dilluns es duu a terme el darrer Consell de Govern del meu mandat com a rector; el proper dia 6 de maig, com correspon, hi haurà una nova elecció on tota la comunitat universitària podrà escollir nou rector o rectora. Aquest darrer consell té, naturalment, un caràcter marcadament tècnic; l'ordre del dia complet el trobaràs adjunt al final d'aquest text. A continuació et comento només els punts que, al meu parer, poden ser més del teu interès.

#### Translation (GOOGLE TRANSLATE) to English

Dear and beloved member of the university community, Today is Monday carried out by the Governing Council last of my term as rector, the next day, May 6, as appropriate, there will be another election where the entire university community can choose new rector. This last advice is, of course, a markedly technician complete agenda can be found attached to the end of this text. Then I said only the points that I believe may be of interest.



# Machine Translation System

Input sentence (Benvolguda i benvolgut ...)

Translation system

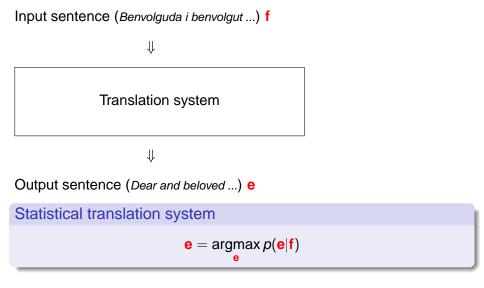
∜

∜

Output sentence (Dear and beloved ...)

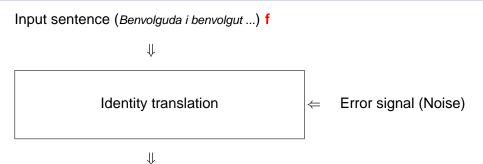


# Machine Translation System





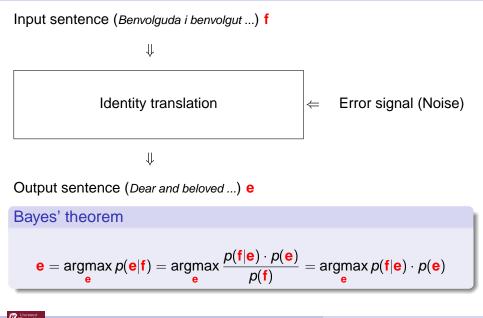
# Noisy Channel Viewpoint



Output sentence (Dear and beloved ...) e



# Noisy Channel Viewpoint



## Components



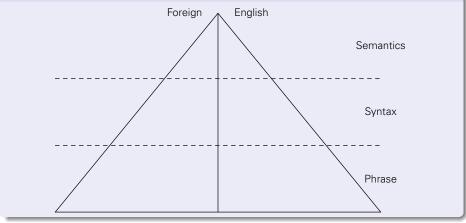
$$\mathbf{e} = \operatorname*{argmax}_{\mathbf{e}} p(\mathbf{f}|\mathbf{e}) \cdot p(\mathbf{e})$$

# Required models • p(e) — language model • p(f|e) — translation model

Input  
Sentence fTranslation  
model 
$$p(f|e)$$
Language  
model  $p(e)$ Output  
sentence e

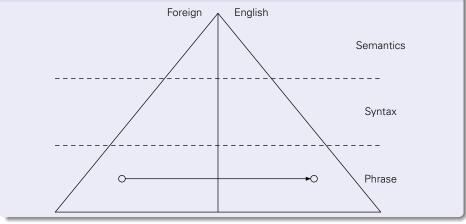






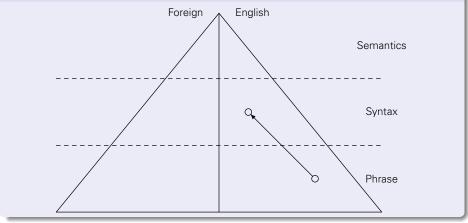






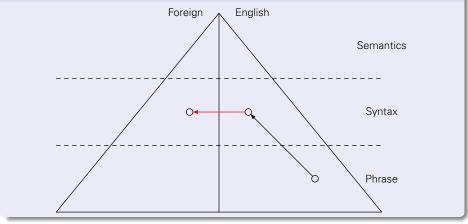






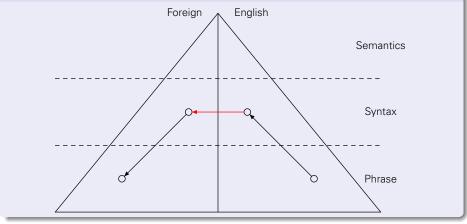














# Why Syntax?

#### Example

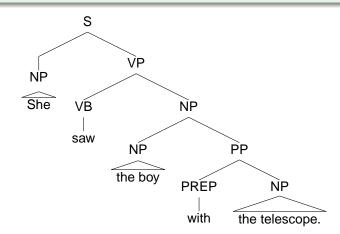
She saw the boy with the telescope.



# Why Syntax?

#### Example

#### She saw the boy with the telescope.

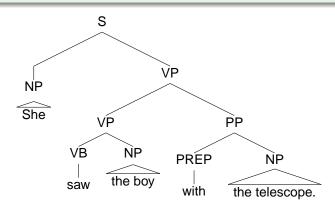




# Why Syntax?

#### Example

#### She saw the boy with the telescope.

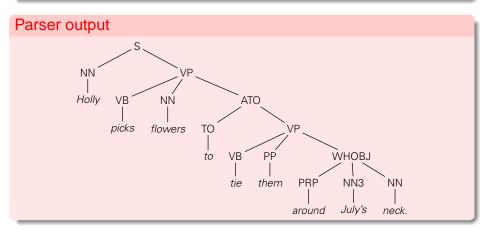




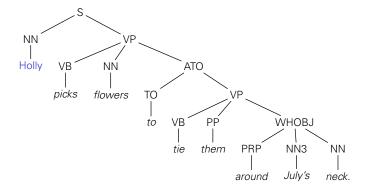
# Syntactic Analysis

#### Output sentence

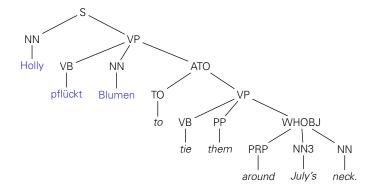
#### Holly picks flowers to tie them around July's neck.



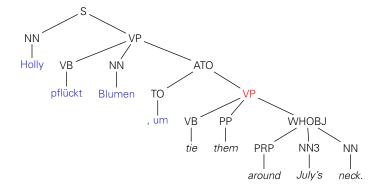




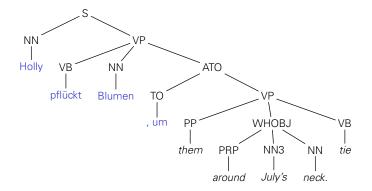




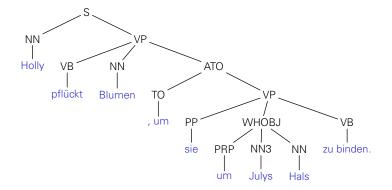














## Table of Contents

## Machine Translation

## Weighted Extended Top-down Tree Transducer

### 3 Expressive Power

## Standard Algorithms

## 5 Implementation



# Weight Structure

#### Definition

 $(A, +, \cdot, 0, 1)$  is a (commutative) semiring if

- (A, +, 0) and  $(A, \cdot, 1)$  commutative monoids,
- distributes over +, and
- $a \cdot 0 = 0$  for every  $a \in A$ .

#### Example

- ( $\{0, 1\}$ , max, min, 0, 1) BOOLEAN semiring
- ( $\mathbb{R}, +, \cdot, 0, 1$ ) semiring of real numbers
- ( $\mathbb{N} \cup \{\infty\}, \min, +, \infty, 0$ )
- any field, ring, etc.



# Syntax

## Definition

 $(Q, \Sigma, \Delta, I, R)$  (weighted) extended (top-down) tree transducer (xtt)

- Q finite set of states
- Σ and Δ ranked alphabets
- I:  $Q \rightarrow A$  initial weight distribution
- *R*: Q(T<sub>Σ</sub>(X)) × T<sub>Δ</sub>(Q(X)) → A is a *rule weight* assignment s.t.
  supp(*R*) is finite and
  for every (*I*, *r*) ∈ supp(*R*) there is *k* ∈ N such that *I* ∈ Q(C<sub>Σ</sub>(X<sub>k</sub>))

and  $r \in T_{\Delta}(Q(X_k))$ .

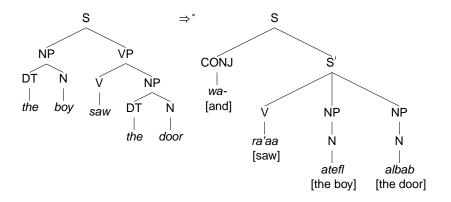
## References

• ARNOLD, DAUCHET: Bi-transductions de forêts. ICALP 1976

• GRAEHL, KNIGHT: Training Tree Transducers. HLT-NAACL 2004



## Syntax — Example



#### Question

How to implement this English  $\rightarrow$  Arabic translation using xtt?



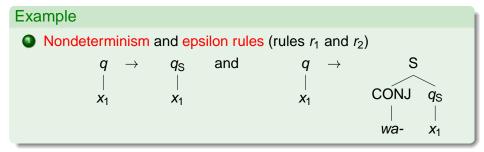
#### Example

q1

States  $\{q, q_{S}, q_{V}, q_{NP}\}$  of which only q is initial

$$\begin{array}{ll} q(x_1) \rightarrow q_{\mathsf{S}}(x_1) & (r_1) \\ q(x_1) \rightarrow \mathsf{S}(\mathsf{CONJ}(\mathit{wa-}), q_{\mathsf{S}}(x_1)) & (r_2) \\ q_{\mathsf{S}}(\mathsf{S}(x_1, \mathsf{VP}(x_2, x_3))) \rightarrow \mathsf{S}'(q_{\mathsf{V}}(x_2), q_{\mathsf{NP}}(x_1), q_{\mathsf{NP}}(x_3)) & (r_3) \\ q_{\mathsf{V}}(\mathsf{V}(\mathit{saw})) \rightarrow \mathsf{V}(\mathit{ra'aa}) & (r_4) \\ q_{\mathsf{NP}}(\mathsf{NP}(\mathsf{DT}(\mathit{the}), \mathsf{N}(\mathit{boy}))) \rightarrow \mathsf{NP}(\mathsf{N}(\mathit{atefl})) & (r_5) \\ q_{\mathsf{P}}(\mathsf{NP}(\mathsf{DT}(\mathit{the}), \mathsf{N}(\mathit{door}))) \rightarrow \mathsf{NP}(\mathsf{N}(\mathit{albab})) & (r_6) \end{array}$$

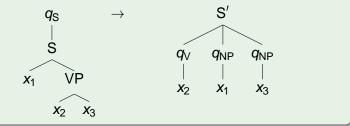






## Example

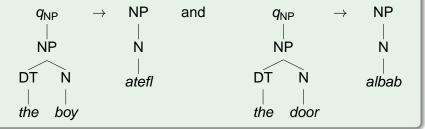
- Nondeterminism and epsilon rules (rules  $r_1$  and  $r_2$ )
- **2** Deep attachment of variables (rule  $r_3$ )





## Example

- Nondeterminism and epsilon rules (rules  $r_1$  and  $r_2$ )
- **2** Deep attachment of variables (rule  $r_3$ )
- Sinite look-ahead (rules  $r_4$  and  $r_5$ )





## Semantics

## Definition

Let  $\xi, \zeta \in T_{\Delta}(Q(T_{\Sigma}))$ . Then  $\xi \stackrel{a}{\Longrightarrow}_{M} \zeta$  if there exist

- a rule  $R(q(t), u) = a \neq 0$
- **2** a substitution  $\theta: X \to T_{\Sigma}$
- 3 a position  $w \in pos(\xi)$

such that  $\xi|_w = q(t\theta)$  and  $\zeta = \xi[u\theta]_w$ 

## Definition

Computed transformation ( $t \in T_{\Sigma}$  and  $u \in T_{\Delta}$ ):

$$\tau_{M}(t, u) = \sum_{\substack{q \in Q \\ q(t) \stackrel{a_{1}}{\longrightarrow} \cdots \stackrel{a_{n}}{\longrightarrow} u \\ \text{left-most derivation}}} l(q) \cdot a_{1} \cdot \ldots \cdot a_{n}$$



## Semantics

## Definition

Let  $\xi, \zeta \in T_{\Delta}(Q(T_{\Sigma}))$ . Then  $\xi \stackrel{a}{\Longrightarrow}_{M} \zeta$  if there exist

- a rule  $R(q(t), u) = a \neq 0$
- **2** a substitution  $\theta: X \to T_{\Sigma}$
- 3 a position  $w \in pos(\xi)$

such that  $\xi|_w = q(t\theta)$  and  $\zeta = \xi[u\theta]_w$ 

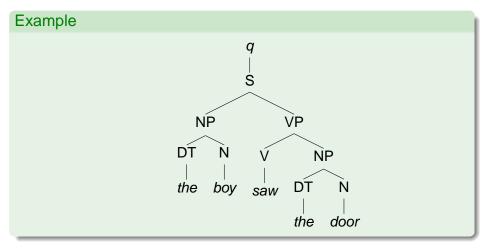
## Definition

Computed transformation ( $t \in T_{\Sigma}$  and  $u \in T_{\Delta}$ ):

$$\tau_{M}(t, u) = \sum_{\substack{q \in Q \\ q(t) \stackrel{a_{1}}{\longrightarrow} \cdots \stackrel{a_{n}}{\Longrightarrow} u \\ \text{left-most derivation}}} I(q) \cdot a_{1} \cdot \ldots \cdot a_{n}$$

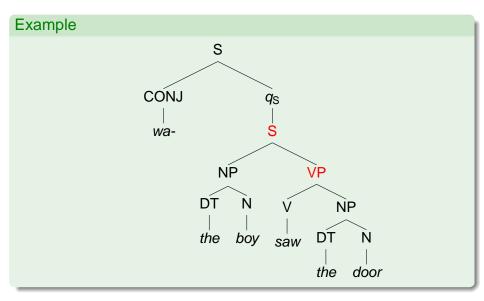


## Semantics — Example

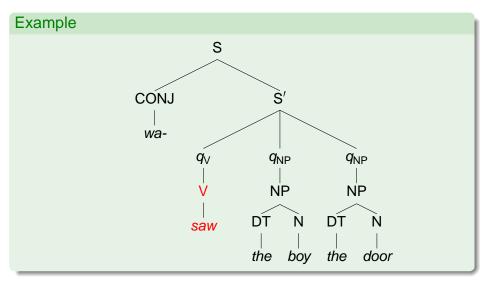




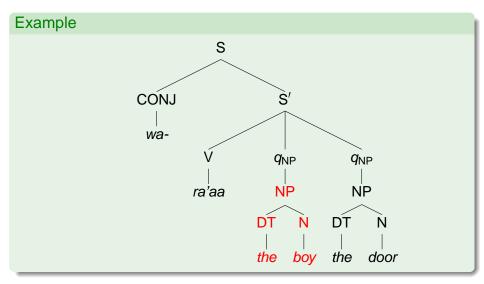
## Semantics — Example



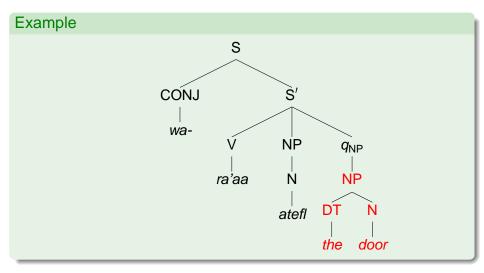




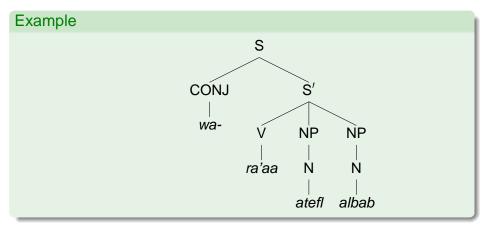














## Table of Contents

Machine Translation

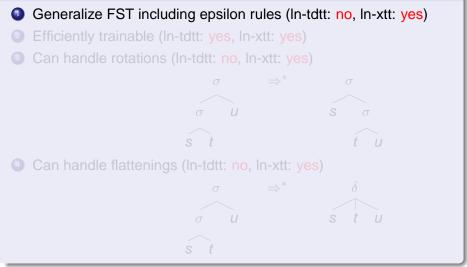
### 2 Weighted Extended Top-down Tree Transducer

3 Expressive Power

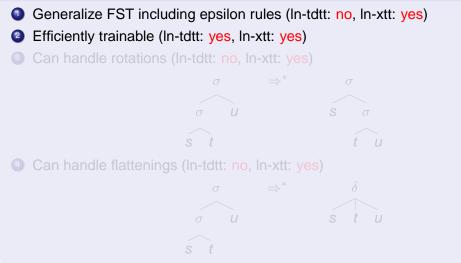
Standard Algorithms

### 5 Implementation



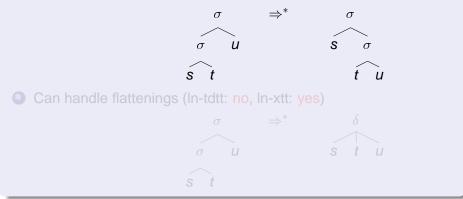






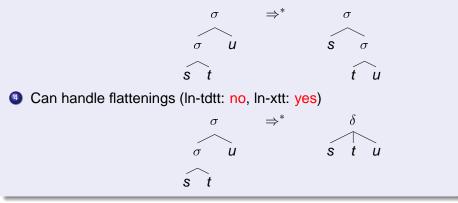


- Generalize FST including epsilon rules (In-tdtt: no, In-xtt: yes)
- Efficiently trainable (In-tdtt: yes, In-xtt: yes)
- Oan handle rotations (In-tdtt: no, In-xtt: yes)





- Generalize FST including epsilon rules (In-tdtt: no, In-xtt: yes)
- 2 Efficiently trainable (In-tdtt: yes, In-xtt: yes)
- Oan handle rotations (In-tdtt: no, In-xtt: yes)





# Wanted Expressivity (Cont'd)

## Criteria

Preservation of Recognizability (In-tdtt: yes, In-xtt: yes)

Closure under composition (In-tdtt: yes, In-xtt: no)

### Definition

- linear: no right-hand side contains a duplicate variable
- non-deleting: all right-hand sides contain all variables of their left-hand side
- epsilon-free: no rules of the form  $q(x) \rightarrow u$



# Wanted Expressivity (Cont'd)

## Criteria

Preservation of Recognizability (In-tdtt: yes, In-xtt: yes)

Closure under composition (In-tdtt: yes, In-xtt: no)

### Definition

- linear: no right-hand side contains a duplicate variable
- non-deleting: all right-hand sides contain all variables of their left-hand side
- epsilon-free: no rules of the form  $q(x) \rightarrow u$



## Features of xtt

### **Discriminative features**

- Finite look-ahead
- Epsilon rules
- Deep attachment of variables



## Features of xtt

### **Discriminative features**

- Finite look-ahead
- Epsilon rules
- Deep attachment of variables



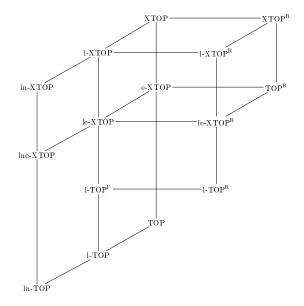
## Features of xtt

### **Discriminative features**

- Finite look-ahead
- Epsilon rules
- Deep attachment of variables



## Hasse Diagram (if the weight structure is not a ring)





## Table of Contents

Machine Translation

2 Weighted Extended Top-down Tree Transducer

3 Expressive Power



#### 5 Implementation



## Composition

#### Theorem

Every 1-TOP  $\subseteq \mathcal{L} \subseteq$  XTOP is not closed under composition.

### Proof.

Composition closure of 1-TOP is 1-TOP<sup>R</sup>. By the diagram, 1-TOP<sup>R</sup>  $\not\subseteq$  XTOP.

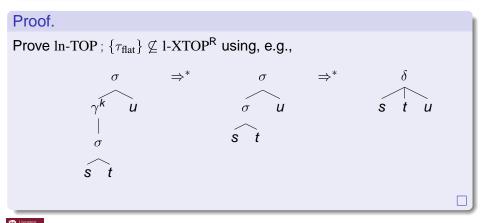
#### Reference

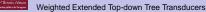
• ARNOLD, DAUCHET: Morphismes et bimorphismes d'arbres. Theoret. Comput. Sci. 20, 1982



#### Theorem

Every  $\ln$ -TOP  $\subseteq \mathcal{L} \subseteq 1$ -XTOP<sup>*R*</sup> that contains rotations or flattenings is not closed under composition.





#### Theorem

XTOP<sup>*R*</sup> is not closed under composition.

#### Proof.

Follow classical proof for TOP<sup>R</sup>.

#### **Conclusion or Bad news**

No (mentioned) class of xtt computes a closed class of transformation.



#### Theorem

XTOP<sup>*R*</sup> is not closed under composition.

#### Proof.

Follow classical proof for TOP<sup>R</sup>.

#### Conclusion or Bad news

No (mentioned) class of xtt computes a closed class of transformation.



#### Problem

Compositions are extremely important (e.g., for a framework)!

### Questions

- Identify suitable subclasses that are closed under composition (expressive vs. closure)
- Otermine whether two given I-xtt can be composed
- What is the composition closure of I-XTOP
- Identify superclasses that are closed under composition and still preserve recognizability (preservation vs. closure)

#### Reference

• ~, GRAEHL, HOPKINS, KNIGHT: The power of extended top-down tree transducers. SIAM J. Comput. 39, 2009



#### Problem

Compositions are extremely important (e.g., for a framework)!

### Questions

- Identify suitable subclasses that are closed under composition (expressive vs. closure)
- Oetermine whether two given I-xtt can be composed
- What is the composition closure of I-XTOP
- Identify superclasses that are closed under composition and still preserve recognizability (preservation vs. closure)

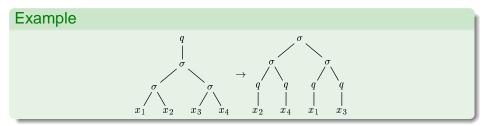
#### Reference

• ~, GRAEHL, HOPKINS, KNIGHT: The power of extended top-down tree transducers. SIAM J. Comput. 39, 2009

## **Binarization**

### Definition

#### A xtt is binarized if there are at most 3 states per rule.



#### Conclusions

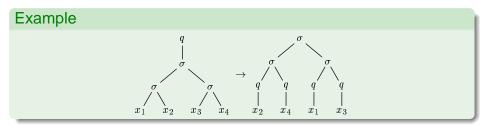
- linear xtt are not binarizable [Ано, ULLMAN 1972]
- What about non-linear xtt?



## **Binarization**

### Definition

A xtt is binarized if there are at most 3 states per rule.

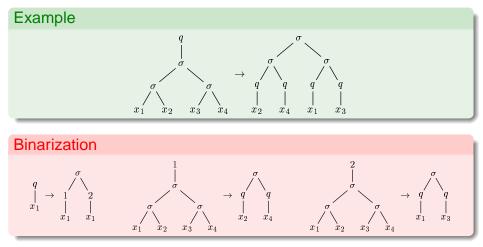


### Conclusions

- linear xtt are not binarizable [Ано, ULLMAN 1972]
- What about non-linear xtt?



# Binarization (Cont'd)



 $\Rightarrow$  Non-linear xtt can be binarized.



## Input Product

#### Definition

Given 
$$\tau : T_{\Sigma} \times T_{\Delta} \to A$$
 and  $\varphi : T_{\Sigma} \to A$ , let  $\varphi \triangleleft \tau : T_{\Sigma} \times T_{\Delta} \to A$ 

$$(\varphi \triangleleft \tau)(t, u) = \varphi(t) \cdot \tau(t, u)$$

#### Theorem

 $\varphi \triangleleft \tau \in \mathsf{n-XTOP}$  for every  $\varphi \in \mathsf{Rec} \text{ and } \tau \in \mathsf{n-XTOP}$ 



## Input Product (Cont'd)

## Parsing complexity

In-xtt *M* and input word *w*:  $O(|M| \cdot |w|^{2 \operatorname{rk}(M)+5})$ 

### References

- ~, SATTA: Unpublished manuscript, 2010
- ~: Why synchronous tree substitution grammars? HLT-NAACL 2010



## Input Product (Cont'd)

### **Deleting xtt**

How to obtain input products for deleting xtt?

### Partial solutions

- for idempotent semirings
- for rings

but they do not work for xtt after binarization

#### References

 ~: Input products for weighted extended top-down tree transducers. DLT 2010



## Input Product (Cont'd)

### **Deleting xtt**

How to obtain input products for deleting xtt?

### Partial solutions

- for idempotent semirings
- for rings

but they do not work for xtt after binarization

#### References

 ~: Input products for weighted extended top-down tree transducers. DLT 2010



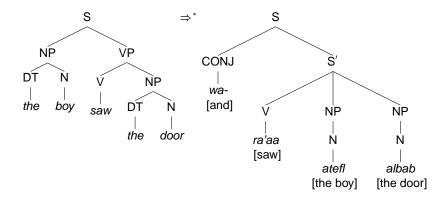
handled in a later talk

#### References

- Fülöp, ~, Vogler: Backward and forward application of extended tree series transformations. WATA 2010
- May, Knight, Vogler: Efficient inference through cascades of weighted tree transducers. ACL 2010



# Training

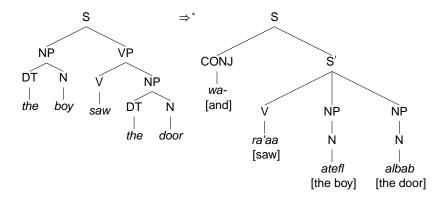


#### Reference

• GRAEHL, KNIGHT, MAY: Training Tree Transducers. Comput. Ling. 34(3), 2008



# Training

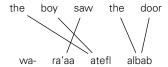


#### Reference

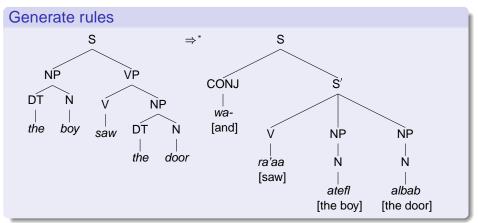
• GRAEHL, KNIGHT, MAY: Training Tree Transducers. Comput. Ling. 34(3), 2008



# Training (Cont'd)

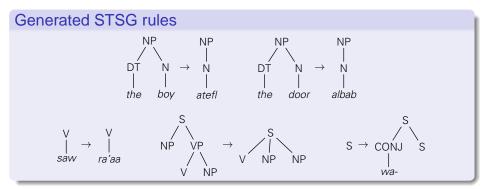


#### Alignment





# Training (Cont'd)

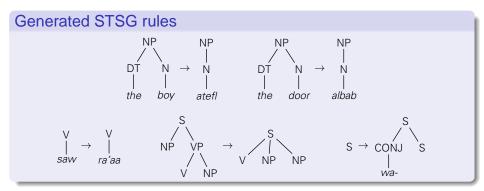


#### Conclusion

- In-xtt efficiently trainable
- Can we use states? Nonlinearity? Deletion? ...



# Training (Cont'd)



### Conclusion

- In-xtt efficiently trainable
- Can we use states? Nonlinearity? Deletion? ...



## Table of Contents

- Machine Translation
- 2 Weighted Extended Top-down Tree Transducer
- 3 Expressive Power
- Standard Algorithms





## Tiburon

#### Features

- Implements xtt (and tree automata; everything also weighted)
- Framework with command-line interface
- Optimized for machine translation

## Algorithms

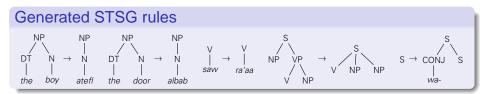
- Application of xtt to input tree/language
- Backward application of xtt to output language
- Composition (for some xtt)
- . . .

## Reference

• MAY, KNIGHT: Tiburon: A Weighted Tree Automata Toolkit. CIAA 2006



# Tiburon (Cont'd)



#### Example

q		
qNP.NP(DT(the) N(boy))	->	NP(N(atefl))
qNP.NP(DT(the) N(door))	->	NP(N(albab))
qV.V(saw)	->	V(ra'aa)
qS.S(x0: VP(x1: x2:))	->	S(qV.x1 qNP.x0 qNP.x2)
q.x0:	->	S(CONJ(wa-) qS.x0)



# Summary

## Criteria

- (a) Generalize FST; in particular, epsilon-transitions
- (b) Efficient training
- (c) Handles rotation
- (d) Closed under composition
- (e) Preserves recognizability

## Models

Model \ Criterion	(a)	(b)	(c)	(d)	(e)
Top-down tree transducer	_	Х	—	Х	Х
Synchronous context-free grammar	х	х	—	х	х
Synchronous tree substitution grammar	х	х	х	_	х
Synchronous tree adjoining grammar	х	х	х	_	_
Multi bottom-up tree transducer	х	?	х	х	_



## References

- ARNOLD, DAUCHET: Bi-transductions de forêts. ICALP 1976
- BAKER: Composition of top-down and bottom-up tree transducers. *Inform. Control 41*. 1979
- ENGELFRIET: Bottom-up and top-down tree transformations—a comparison. *Math. Syst. Theory 9.* 1975
- ENGELFRIET: Top-down tree transducers with regular look-ahead. *Math. Syst. Theory 10.* 1976
- MAY, KNIGHT: Tiburon: A Weighted Tree Automata Toolkit. CIAA 2006
- $\sim$ , GRAEHL, HOPKINS, KNIGHT: The power of extended top-down tree transducers. SIAM J. Comput. 2009

# Thank You for your attention!

