

Tree Transducers in Machine Translation

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Machine translation

Applications

- **Technical manuals**

Example (An mp3 player)

The synchronous manifestation of lyrics is a procedure for can broadcasting the music, waiting the mp3 file at the same time showing the lyrics.

With the this kind method that the equipments that synchronous function of support up broadcast to make use of document create setup, you can pass the LCD window way the check at the document contents that broadcast.

That procedure returns offerings to have to modify, and delete, and stick top , keep etc. edit function.

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Machine translation

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- **TripAdvisor**[®]

Example (Hotel Uppsala, Sweden)

Wir hatten die Zimmer eingestuft wird als “Superior” weil sie renoviert wurde im letzten Jahr oder zwei. Unsere Zimmer hatten Parkettboden und waren sehr geräumig. Man musste allerdings nicht musste seitwärts bewegen.

Machine translation

Applications

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Example (Hotel Uppsala, Sweden)

Nos alojamos en habitaciones clasificado como “superior” porque se lo habían renovado en el año pasado o dos. Nuestras habitaciones tenían suelos de madera y eran espaciosas. No te tenías que caminar arriba para movernos por allí.

Machine translation

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Example (Hotel Uppsala, Sweden)

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— *We stayed in rooms classified as “superior” because they had been renovated in the last year or two. Our rooms had wood floors and were roomy. You didn’t have to walk sideways to move around.*

Machine translation

Applications

- Technical manuals
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- **Military**

Example (JONES, SHEN, HERZOG 2009)

Soldier: Okay, what is your name?

Local: Abdul.

Soldier: And your last name?

Local: Al Farran.

Machine translation

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Speech-to-text machine translation

Soldier: Okay, what's your name?

Local: milk a mechanic and I am here
I mean yes

Machine translation

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Speech-to-text machine translation

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I mean yes

Soldier: What is your last name?

Local: every two weeks
my son's name is ismail

Machine translation

Applications

- Technical manuals
- TripAdvisor[®]
- Military
- MSDN, Knowledge Base
- ...

Machine translation (cont'd)

Systems

- GOOGLE translate translate.google.com
- BING translator www.microsofttranslator.com
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Try them!

Machine translation (cont'd)

History

1 Dark age (60s–90s)

- ▶ rule-based systems (e.g., SYSTRAN)
- ▶ CHOMSKYAN approach
- ▶ perfect translation, poor coverage

2 Reformation (1991–present)

- ▶ word-based, phrase-based, syntax-based systems
- ▶ statistical approach
- ▶ cheap, automatically trained

3 Potential future

- ▶ semantics-based systems (e.g., FRAMENET)
- ▶ semi-supervised, statistical approach
- ▶ basic understanding of translated text

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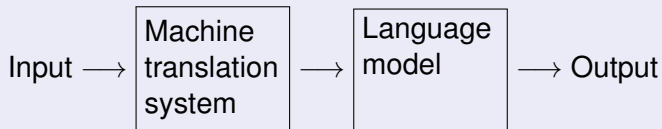
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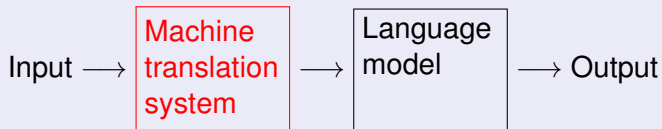
Machine translation (cont'd)

Schema



Machine translation (cont'd)

Schema



Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

And then the matter was decided , and everything was put in place

Output:

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

The diagram illustrates the segmentation of the sentence "And then the matter was decided , and everything was put in place" into a sequence of tokens: f, kAn, An, tm, AlHsm, w, wDEt, Almwr, fy, nSAb, hA. Blue lines connect the words in the sentence to their corresponding tokens, showing a one-to-one mapping.

Derivation

Input:

then *the matter was decided , and everything was put in place*

Output:

Word-based system (FST)

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Derivation

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the *matter was decided , and everything was put in place*

Output:

f

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Word-based system (FST)

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The diagram illustrates the mapping between words and phonetic symbols. The words are: *And*, *then*, *the*, *matter*, *was*, *decided*, *,*, *and*, *everything*, *was*, *put*, *in*, *place*. The phonetic symbols are: *f*, *kAn*, *An*, *tm*, *AlHsm*, *w*, *wDEt*, *Almwr*, *fy*, *nSAb*, *hA*. Blue lines connect the words to their phonetic symbols: *And* to *An*, *then* to *tm*, *the* to *f*, *matter* to *AlHsm*, *was* to *w*, *decided* to *wDEt*, *,* to *wDEt*, *and* to *Almwr*, *everything* to *fy*, *was* to *nSAb*, *put* to *hA*, *in* to *hA*, and *place* to *hA*.

Derivation

Input:

the matter was decided , and everything was put in place

Output:

f kAn

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

the matter *, and everything was put in place*

Output:

f kAn An tm AlHsm

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

the matter and *everything was put in place*

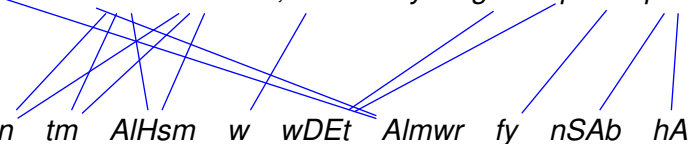
Output:

f kAn An tm AlHsm

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA



Derivation

Input:

the matter *everything* *was put in place*

Output:

f kAn An tm AlHsm w

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

the matter was *put in place*

Output:

f kAn An tm AlHsm w

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

the matter was put in place

Output:

f kAn An tm AlHsm w

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

the matter in *place*

Output:

f kAn An tm AlHsm w wDEt

Word-based system (FST)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

in place

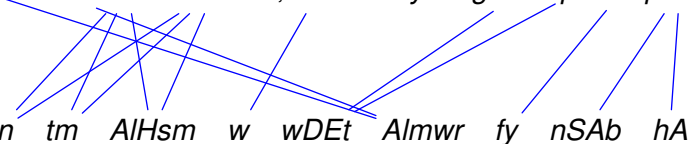
Output:

f kAn An tm AlHsm w wDEt Almwr

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Derivation

Input:

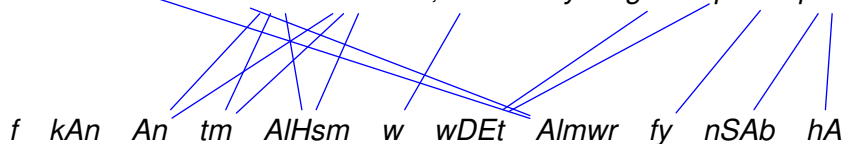
place

Output:

f kAn An tm AlHsm w wDEt Almwr fy

Word-based system (FST)

And then the matter was decided , and everything was put in place



Derivation

Input:

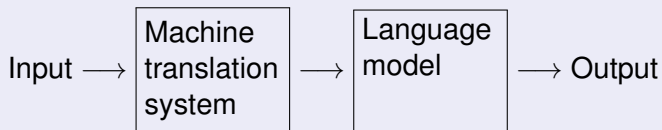


Output:

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Phrase-based machine translation

Schema

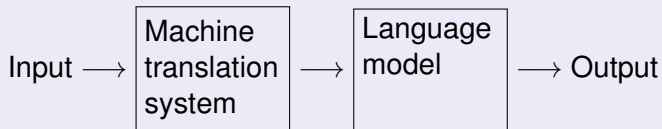


Phrase-based systems

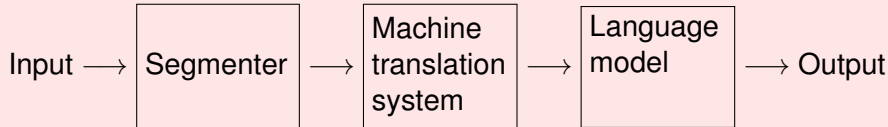


Phrase-based machine translation

Schema



Phrase-based systems



Phrase-based system (FST+Perm)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

And then the matter was decided , and everything was put in place

Output:

Phrase-based system (FST+Perm)

And then the matter was decided , and everything was put in place

f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

*And then*₁ *the matter*₅ *was decided*₂ *, and everything*₃ *was put*₄ *in place*₆

Output:

Phrase-based system (FST+Perm)

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f kAn An tm AlHsm w wDEt Almwr fy nSAb hA

Derivation

Input:

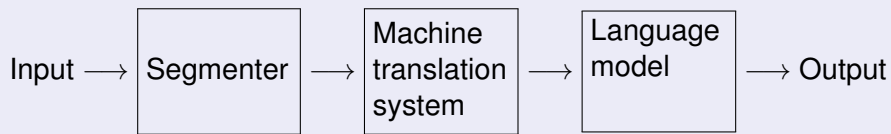
*And then*₁ *the matter*₅ *was decided*₂ *, and everything*₃ *was put*₄ *in place*₆

Output:

*f kAn*₁ *An tm AlHsm*₂ *w*₃ *wDEt*₄ *Almwr*₅ *fy nSAb hA*₆

Machine translation (cont'd)

Phrase-based systems

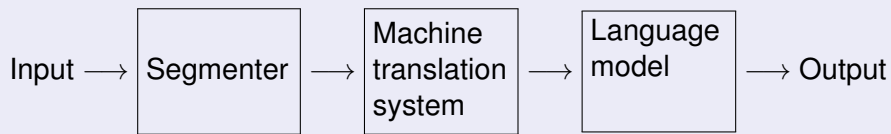


Syntax-based systems

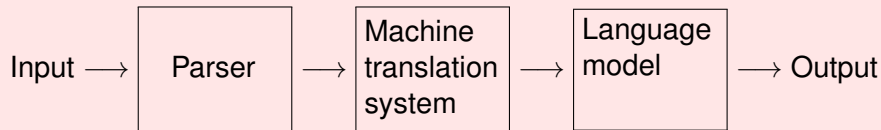


Machine translation (cont'd)

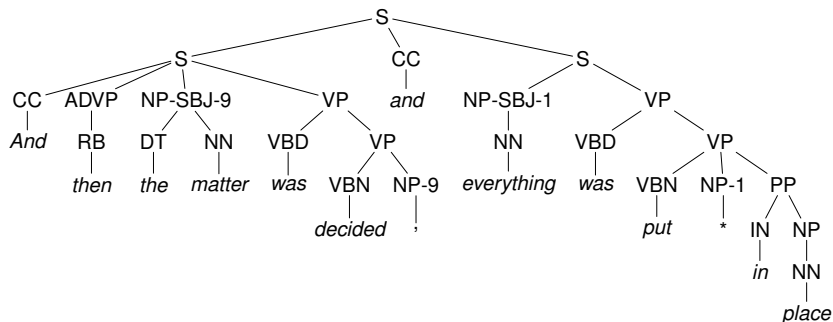
Phrase-based systems



Syntax-based systems

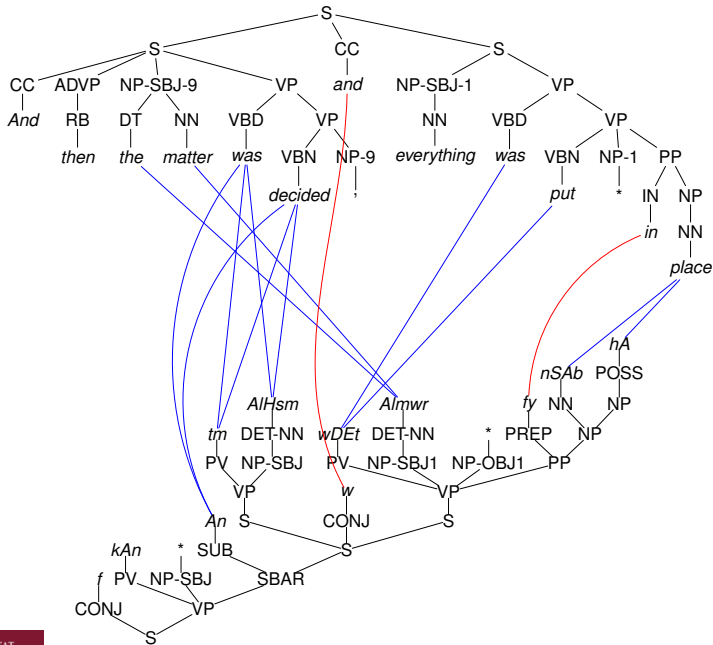


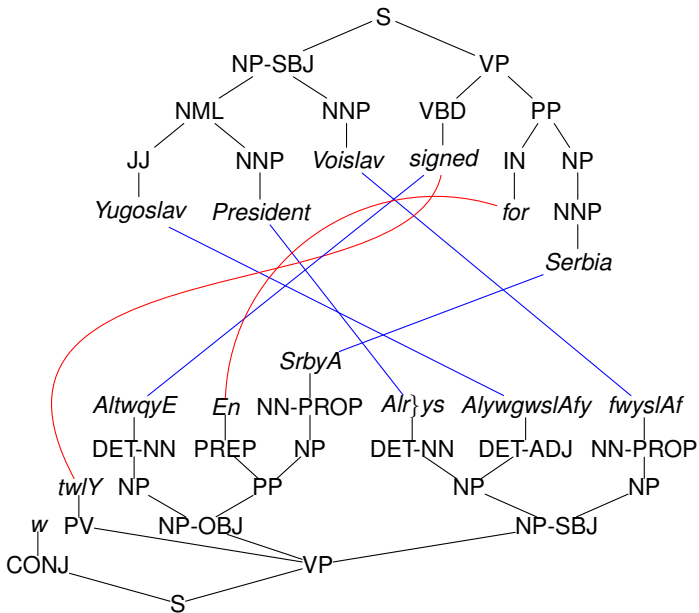
Parser



And then the matter was decided , and everything was put in place

(thanks to [KEVIN KNIGHT](#) for the data)





Contents

- 1 Machine Translation
- 2 Extended Top-down Tree Transducers
- 3 Multi Bottom-up Tree Transducers
- 4 Synchronous Tree-Adjoining Grammars

Weight structure

Definition

Commutative semiring $(C, +, \cdot, 0, 1)$ if

- $(C, +, 0)$ and $(C, \cdot, 1)$ commutative monoids
- \cdot distributes over finite (incl. empty) sums

Example

- BOOLEAN semiring $(\{0, 1\}, \max, \min, 0, 1)$
- Semiring $(\mathbb{R}_{\geq 0}, +, \cdot, 0, 1)$ of probabilities
- Tropical semiring $(\mathbb{N} \cup \{\infty\}, \min, +, \infty, 0)$
- Any field, ring, etc.

Most of the talk: BOOLEAN semiring

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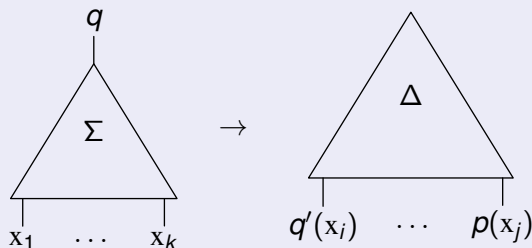
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Syntax

Definition (ARNOLD, DAUCHET 1976, GRAEHL, KNIGHT 2004)

Extended top-down tree transducer (XTOP) $M = (Q, \Sigma, \Delta, l, R)$
with finitely many rules

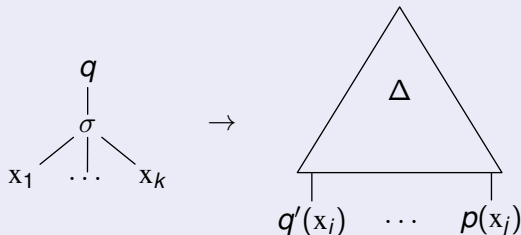


- $q, q', p \in Q$ are states
- $i, j \in \{1, \dots, k\}$

Syntax (cont'd)

Definition (ROUNDS 1970, THATCHER 1970)

- **Top-down tree transducer** (TOP) if all rules

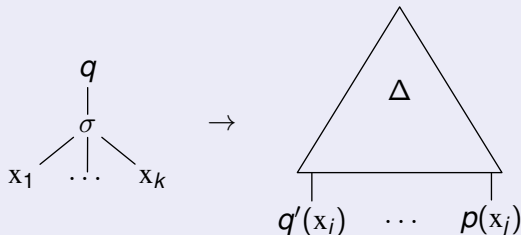


- **linear** if no variable occurs twice in r for all rules $l \rightarrow r$
- **nondeleting** if $\text{var}(l) = \text{var}(r)$ for all rules $l \rightarrow r$

Syntax (cont'd)

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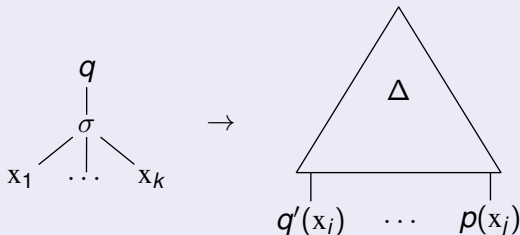


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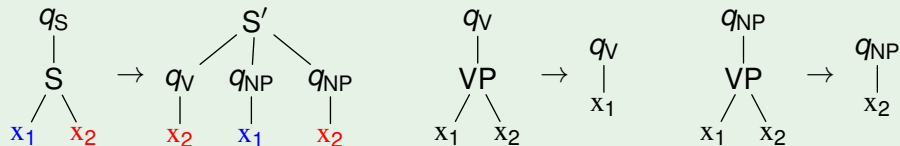


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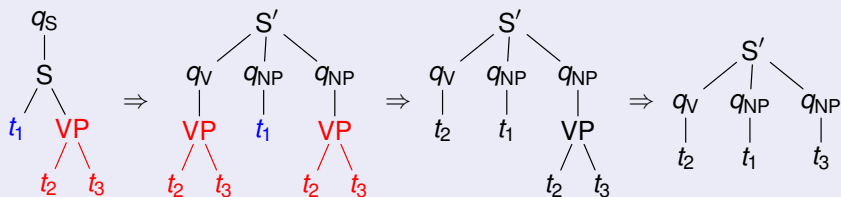
Semantics

Example

States $\{q_S, q_V, q_{NP}\}$ of which only q_S is initial



Derivation

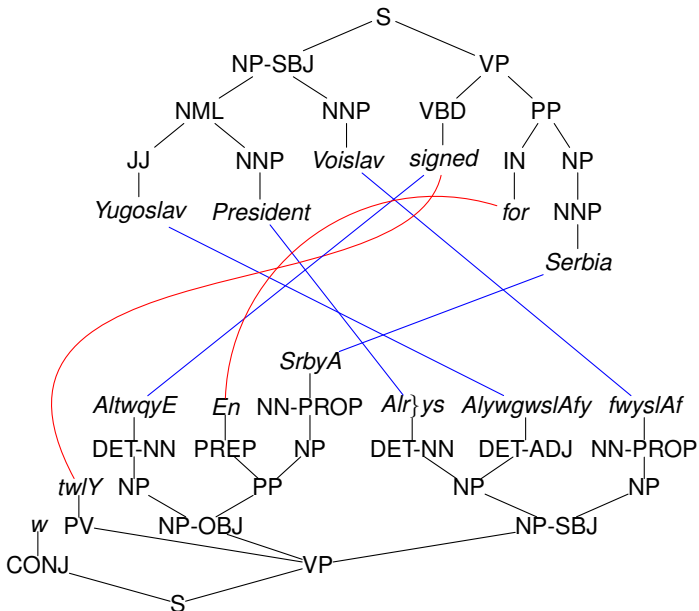


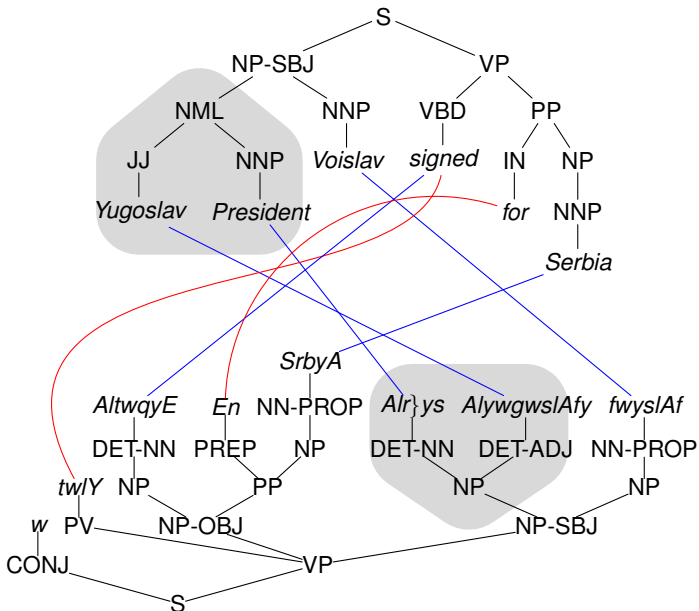
Semantics (cont'd)

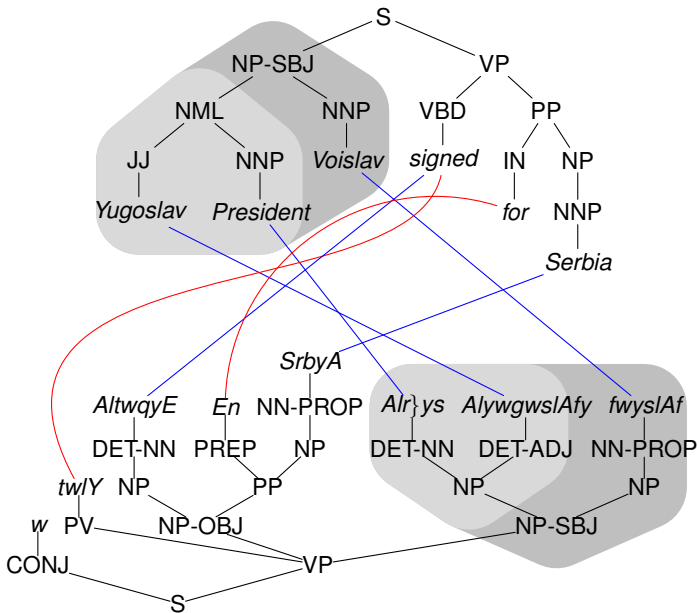
Definition

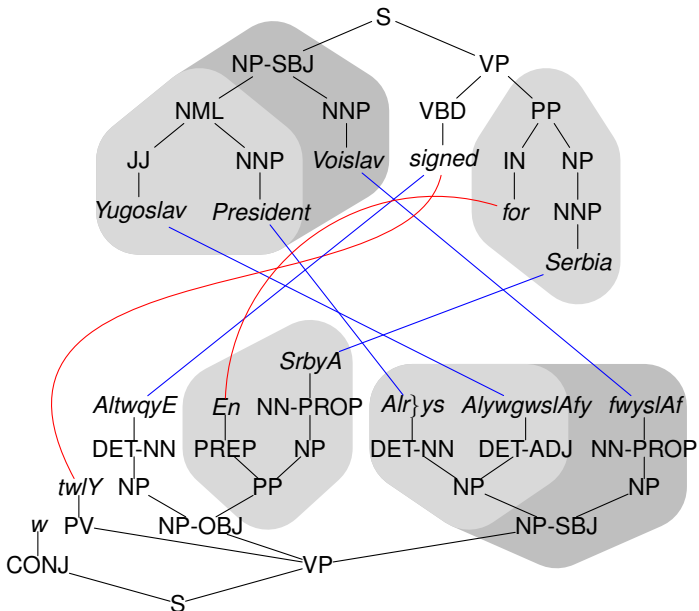
Computed transformation:

$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Delta \mid \exists q \in I: q(t) \Rightarrow^* u\}$$

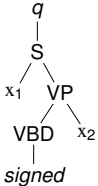
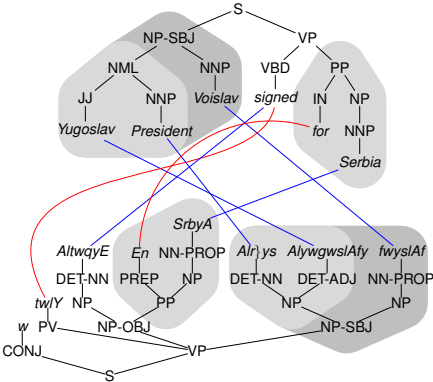




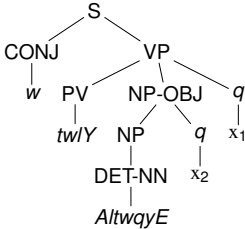




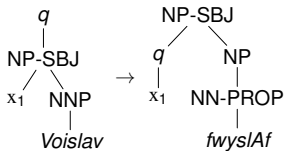
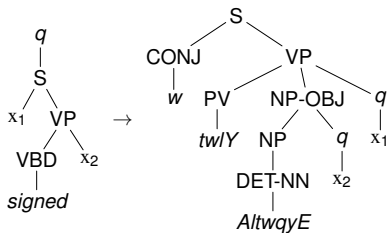
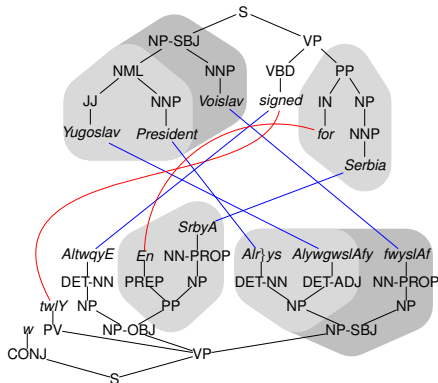
Rule extraction



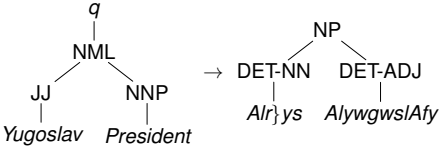
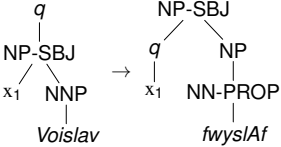
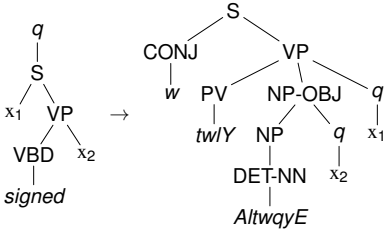
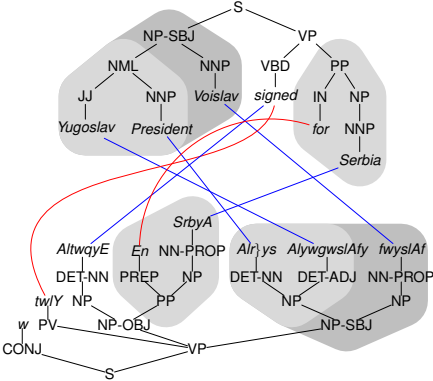
→



Rule extraction

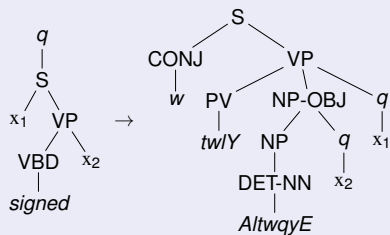


Rule extraction



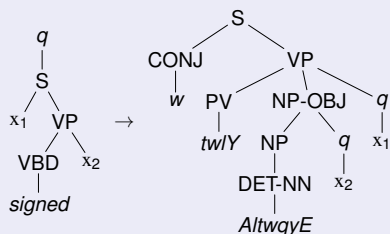
Symmetry

Original rule

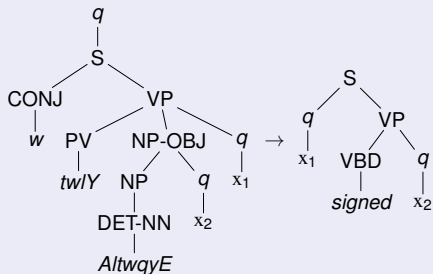


Symmetry

Original rule

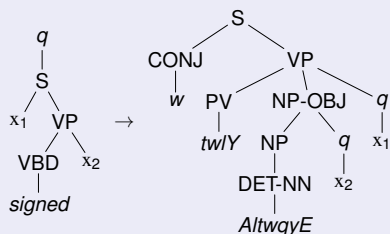


Inverted rule

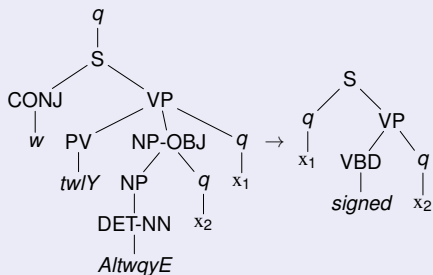


Symmetry

Original rule



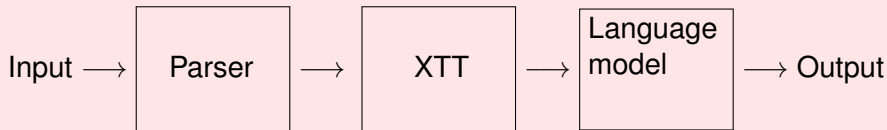
Inverted rule



Linear nondeleting XTT can be inverted

Preservation of regularity

Schematics



Parse trees

- best parse tree
- n -best parses
- all parses

Can all be represented by **regular** tree language

Preservation of regularity

Schematics



Parse trees

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Parse trees

- best parse tree
- n -best parses
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Can all be represented by **regular** tree language

Preservation of regularity (cont'd)

Schematics



Approach

- Input restriction
- Project to output

Result

Linear XTT preserve regularity

Preservation of regularity (cont'd)

Schematics



Approach

- Input restriction
- Project to output

Result

Linear XTT preserve regularity

Preservation of regularity (cont'd)

Schematics



Approach

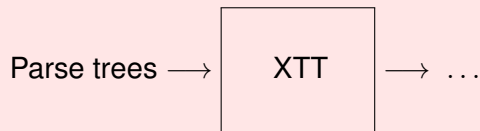
- Input restriction
- Project to output

Result

Linear XTT preserve regularity

Composition

Schematics

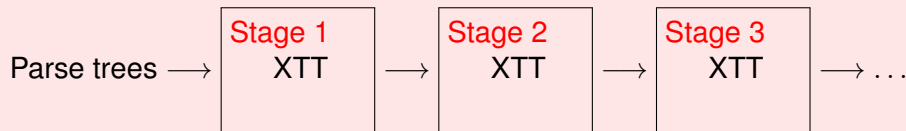


Example (YAMADA, KNIGHT 2002)

- Reorder
- Insert words
- Translate words

Composition

Schematics

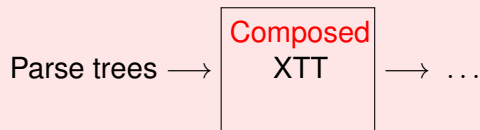


Example (YAMADA, KNIGHT 2002)

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Composition

Schematics

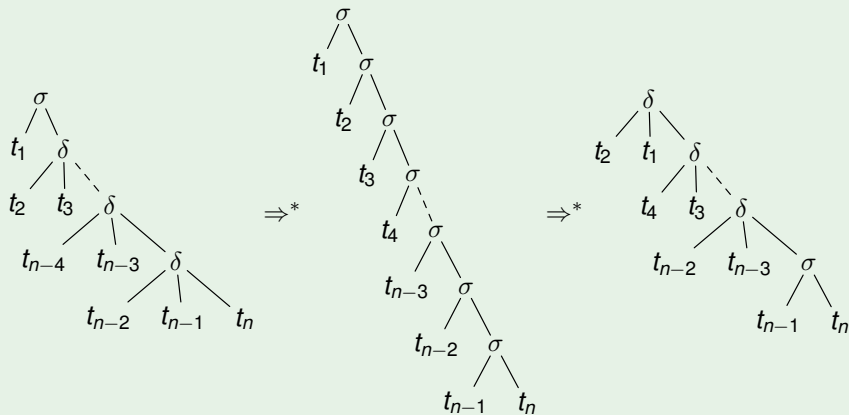


Example (YAMADA, KNIGHT 2002)

- Reorder
- Insert words
- Translate words

Composition (cont'd)

Example (ARNOLD, DAUCHET 1982)



Summary

Model \ Criterion	EXPR	SYM	PRES	PRES ⁻¹	COMP
Linear nondeleting TOP	X	X	✓	✓	✓
Linear TOP	X	X	✓	✓	X
Linear TOP ^R	X	X	✓	✓	✓
General TOP	X	X	X	✓	X
General TOP ^R	✓	X	X	✓	X
Linear nondeleting XTOP	✓	✓	✓	✓	X
Linear XTOP	✓	X	✓	✓	X
Linear XTOP ^R	✓	X	✓	✓	X
General XTOP	✓	X	X	✓	X
General XTOP ^R	✓	X	X	✓	X

Summary

Model \ Criterion	EXPR	SYM	PRES	PRES ⁻¹	COMP
Linear nondeleting TOP	X	X	✓	✓	✓
Linear TOP	X	X	✓	✓	X
Linear TOP ^R	X	X	✓	✓	✓
General TOP	X	X	X	✓	X
General TOP ^R	✓	X	X	✓	X
Linear nondeleting XTOP	✓	✓	✓	✓	X
Linear XTOP	✓	X	✓	✓	X
Linear XTOP ^R	✓	X	✓	✓	X
General XTOP	✓	X	X	✓	X
General XTOP ^R	✓	X	X	✓	X
Comp. closure In-XTOP	✓	✓	✓	✓	✓
“composable” In-XTOP	?	?	✓	✓	✓

Implementation

TIBURON [MAY, KNIGHT 2006]

- Implements XTOP (and tree automata; everything also weighted)
- Framework with command-line interface
- Optimized for machine translation

Algorithms

- Application of XTOP to input tree/language
- Backward application of XTOP to output language
- Composition (for some XTOP)

Example

$qNP . NP (DT (the) N (boy)) \rightarrow NP (N (atefl))$

Implementation

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Implementation

TIBURON [MAY, KNIGHT 2006]

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- Framework with command-line interface
- Optimized for machine translation

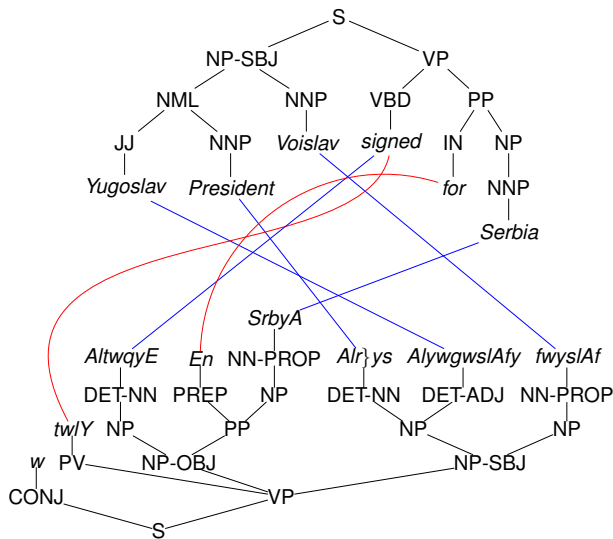
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Example

$qNP.NP (DT (the) N (boy)) \rightarrow NP (N (atefl))$

Multi Bottom-up Tree Transducers

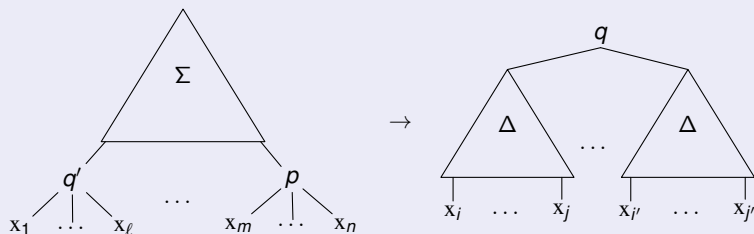


Syntax

Definition

Extended multi bottom-up tree transducer (XMBOT)

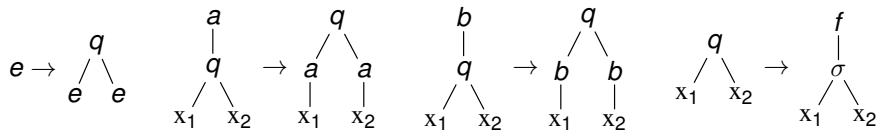
is $M = (Q, \Sigma, \Delta, F, R)$ with finitely many rules



- $q', p, q \in Q$ are now **ranked states**
- $F \subseteq Q_1$ final states

Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

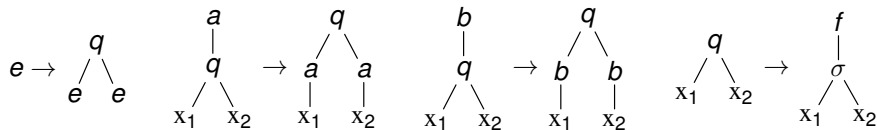


Example (Derivation)

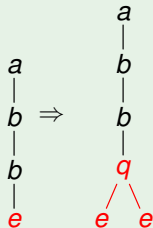
a
|
b
|
b
|
e

Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

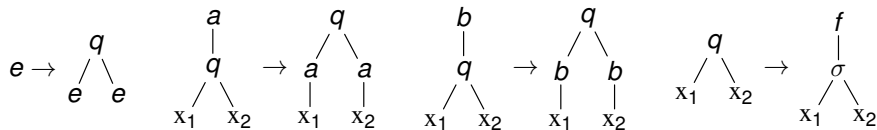


Example (Derivation)

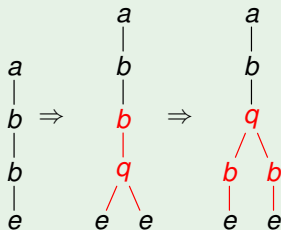


Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

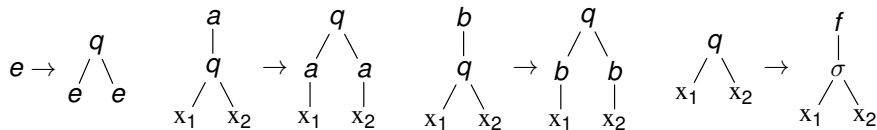


Example (Derivation)

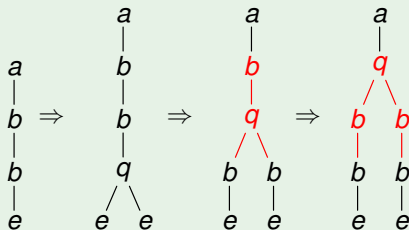


Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

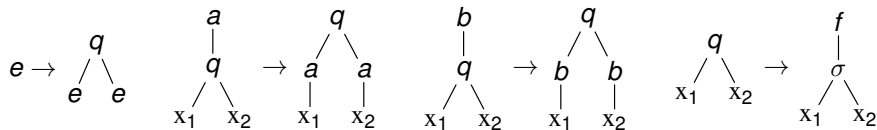


Example (Derivation)

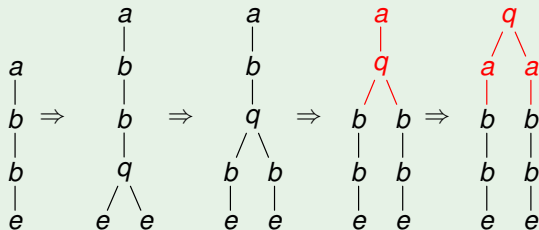


Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

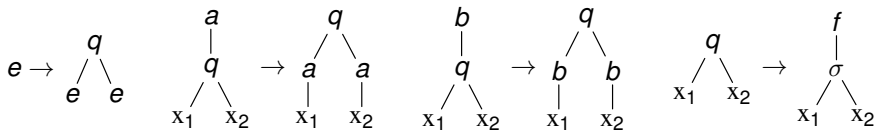


Example (Derivation)

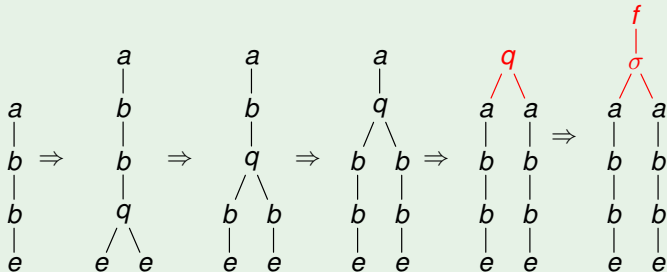


Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules



Example (Derivation)



Definition

Computed transformation:

$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Delta \mid \exists q \in F: t \Rightarrow^* q(u)\}$$

Semantics

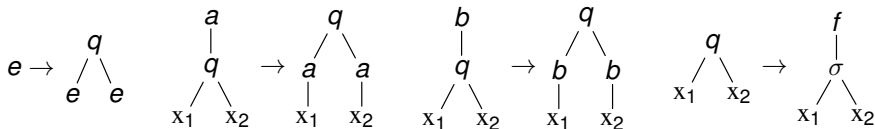
Definition

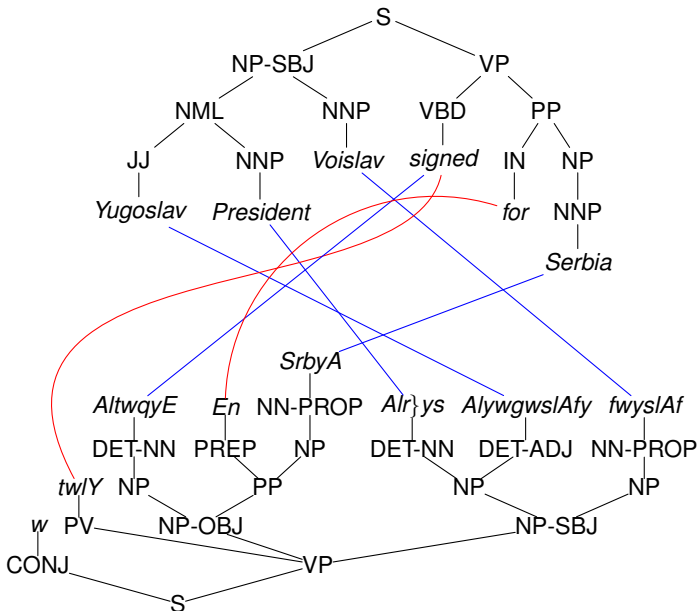
Computed transformation:

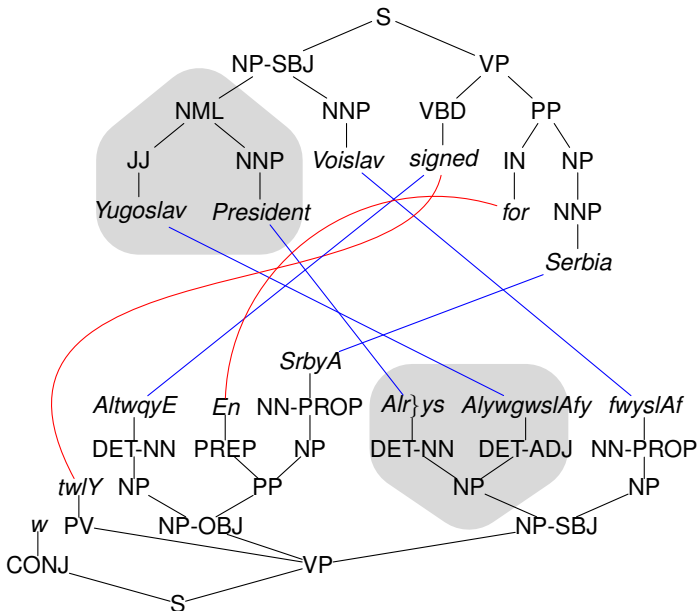
$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Delta \mid \exists q \in F: t \Rightarrow^* q(u)\}$$

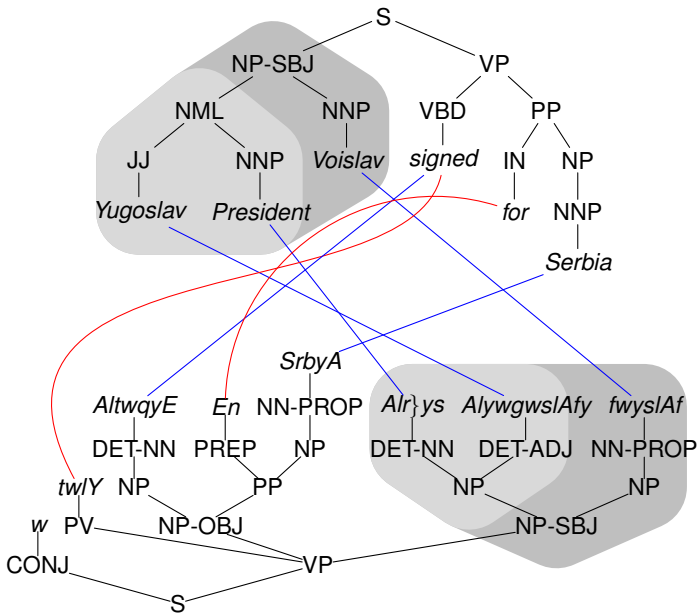
Example

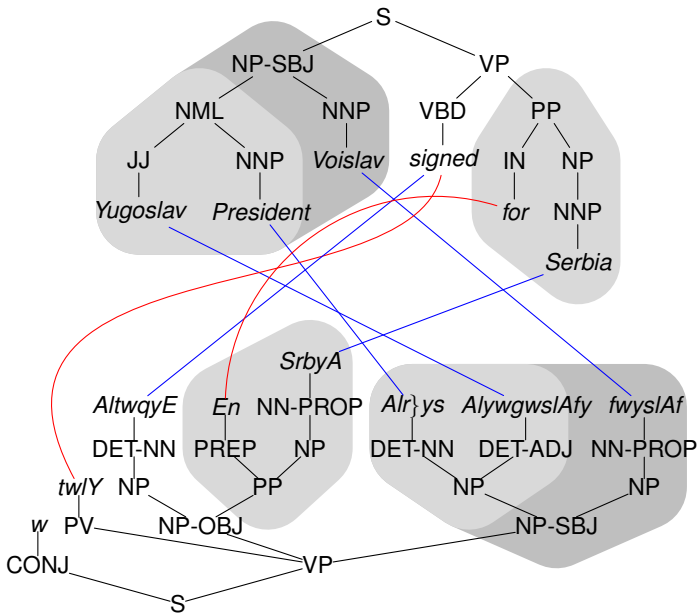
$$\tau_M = \{\langle t, \sigma(t, t) \rangle \mid t \in T_\Sigma\}$$

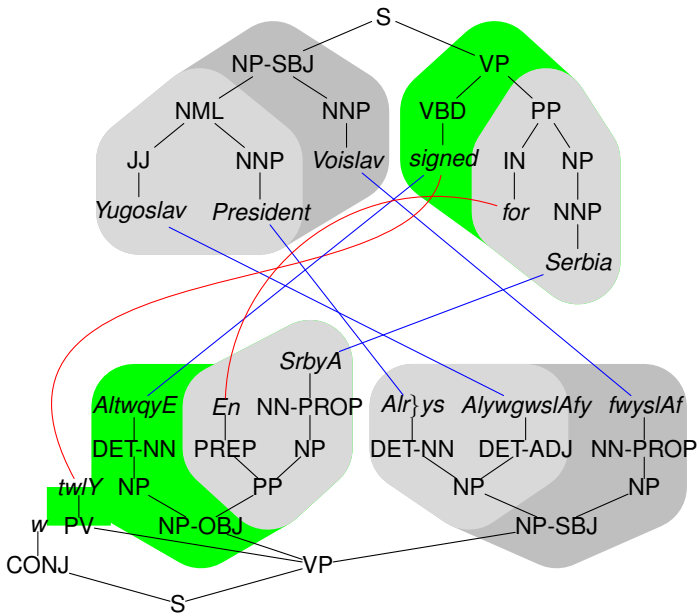




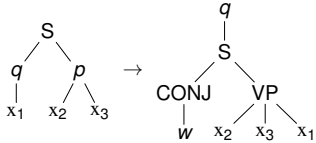
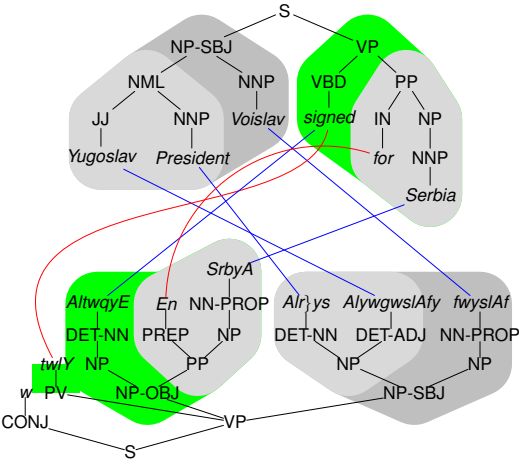




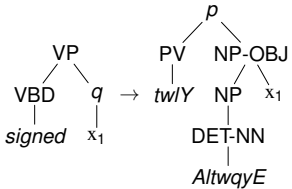
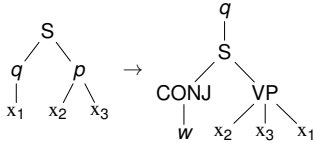
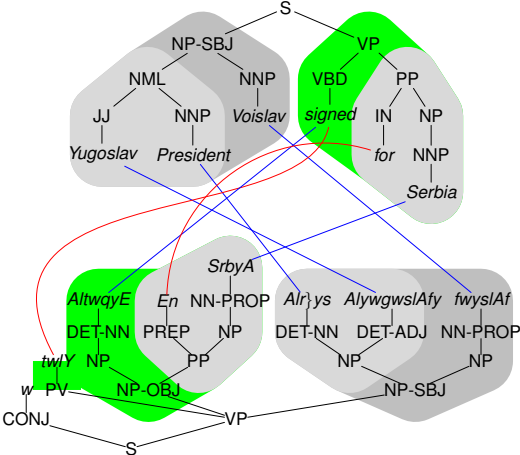




Rule extraction



Rule extraction



One-symbol normal form

Definition

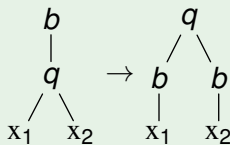
Rule in **one-symbol normal form** if it contains at most one symbol

One-symbol normal form

Definition

Rule in **one-symbol normal form** if it contains at most one symbol

Example (ENGELFRIET, LILIN, ~ 2009)

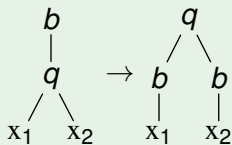


One-symbol normal form

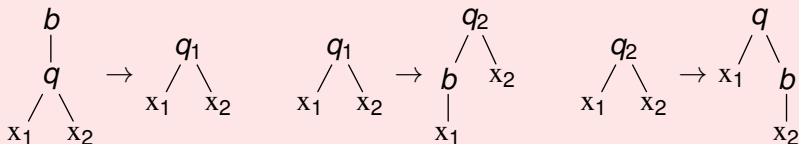
Definition

Rule in **one-symbol normal form** if it contains at most one symbol

Example (ENGELFRIET, LILIN, ~ 2009)



In one-symbol normal form



Basic properties

Example (Copying translation)

$$\tau_M = \{ \langle t, \sigma(t, t) \rangle \mid t \in \mathcal{T}_\Sigma \}$$

Consequences

- XMBOT are not symmetric
- XMBOT do not preserve regularity
- but they can be composed

Basic properties

Example (Copying translation)

$$\tau_M = \{ \langle t, \sigma(t, t) \rangle \mid t \in \mathcal{T}_\Sigma \}$$

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Basic properties

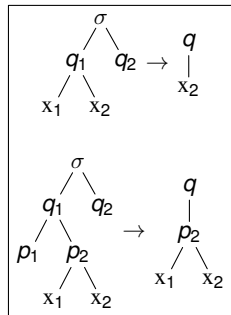
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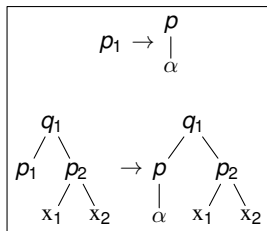
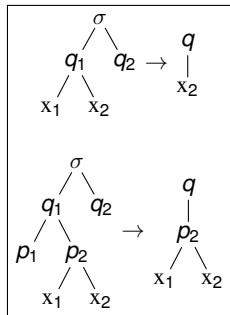
- XMBOT are not symmetric
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- **but they can be composed**

Composition



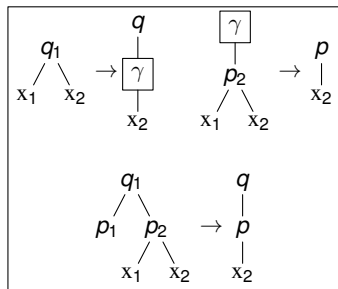
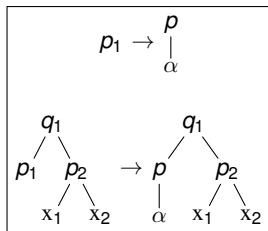
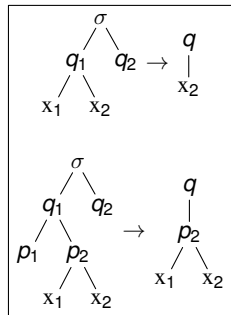
Simple composition works in the typical cases
[BAKER 1979, ENGELFRIET 1975]

Composition



Simple composition works in the typical cases
[BAKER 1979, ENGELFRIET 1975]

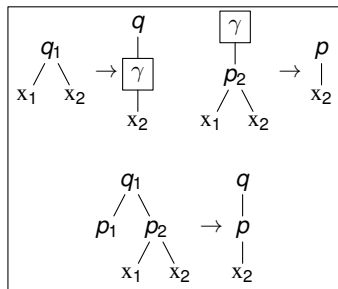
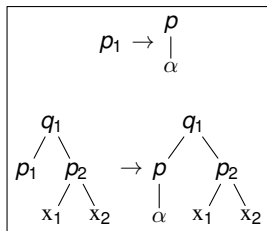
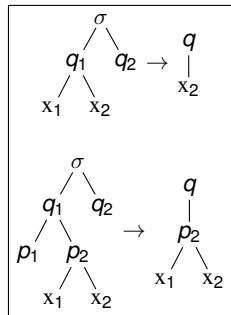
Composition



Simple composition works in the typical cases

[BAKER 1979, ENGELFRIET 1975]

Composition



Simple composition works in the typical cases

[BAKER 1979, ENGELFRIET 1975]

Summary

Model \ Criterion	EXPR	SYM	PRES	$PRES^{-1}$	COMP
Linear nondeleting TOP	✗	✗	✓	✓	✓
Linear nondeleting XTOP	✓	✓	✓	✓	✗
Linear nondeleting XMBOT	✓	✗	✗	✓	✓
Linear XMBOT	✓	✗	✗	✓	✓
General XMBOT	✓	✗	✗	✓	✗
reg.-preserving linear XMBOT	✓	✗	✓	✓	✓
invertable linear XMBOT	✓	✓	✓	✓	✓

Summary

Model \ Criterion	EXPR	SYM	PRES	PRES ⁻¹	COMP
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Linear nondeleting XTOP	✓	✓	✓	✓	✗
Linear nondeleting XMBOT	✓	✗	✗	✓	✓
Linear XMBOT	✓	✗	✗	✓	✓
General XMBOT	✓	✗	✗	✓	✗
reg.-preserving linear XMBOT	✓	✗	✓	✓	✓
invertable linear XMBOT	✓	✓	✓	✓	✓

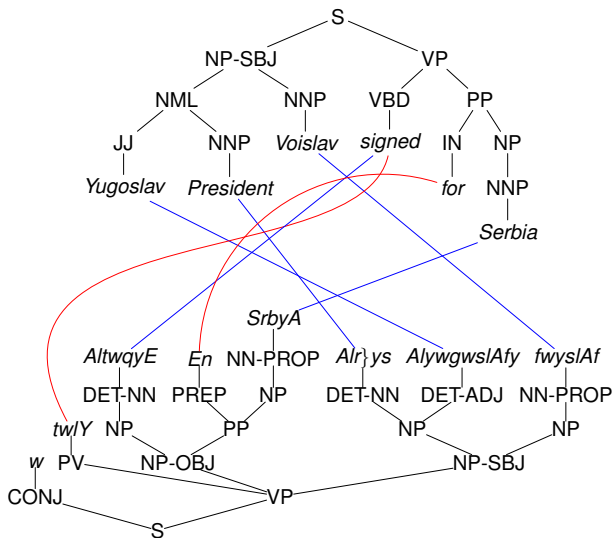
Implementation

No implementation yet,

Implementation

No implementation yet, **but stay tuned**

Synchronous Tree-Adjoining Grammars



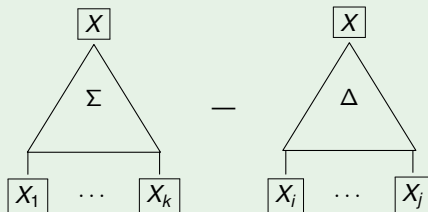
Syntax

Definition (SHIEBER, SCHABES 1990)

Synchronous tree-adjointing grammar (STAG) is $G = (N, \Sigma, \Delta, S, R)$ with a finite set R of

- substitution rules
- adjunction rules

Example (Substitution rule)



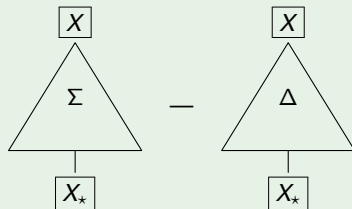
Syntax

Definition (SHIEBER, SCHABES 1990)

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- adjunction rules

Example (Adjunction rule)

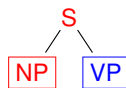
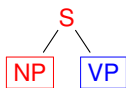


Example

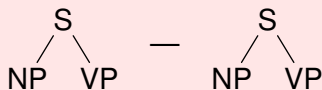
S

S

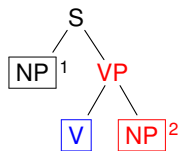
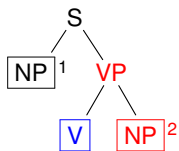
Example



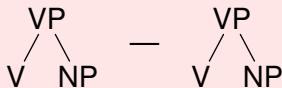
Used substitution rule



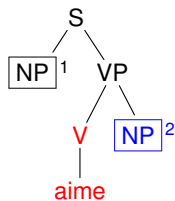
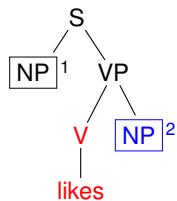
Example



Used substitution rule



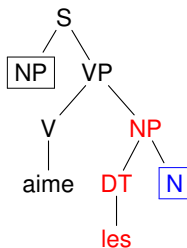
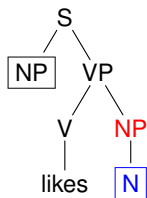
Example



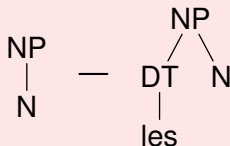
Used substitution rule

V — V
| — |
likes — aime

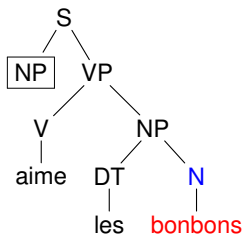
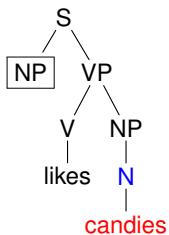
Example



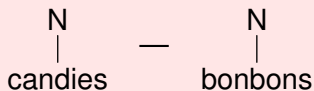
Used substitution rule



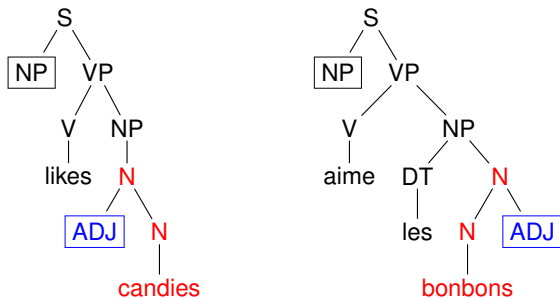
Example



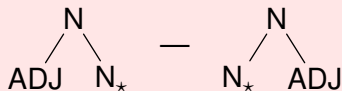
Used substitution rule



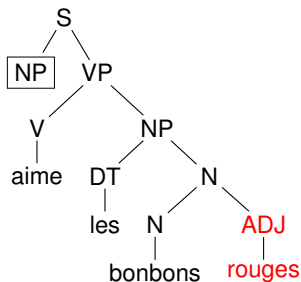
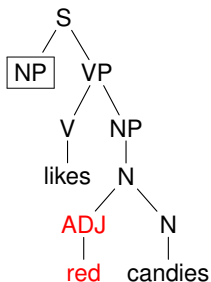
Example



Used adjunction rule



Example



Used substitution rule

ADJ — ADJ
| |
red rouges

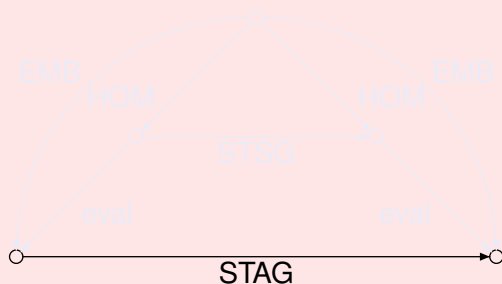
Definition

Computed transformation:

$$\tau_G = \{(t, u) \in T_\Sigma \times T_\Delta \mid (S, S) \Rightarrow^* (t, u)\}$$

Relation to tree transducers

Illustration



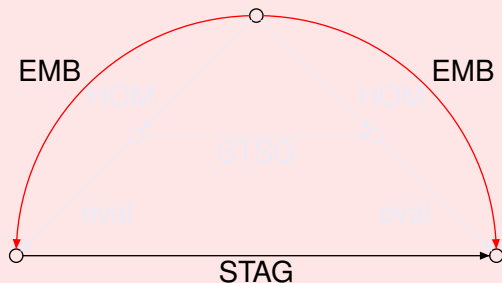
Definition (SHIEBER 2006)

embedded tree transducer is a macro tree transducer:

- linear, nondeleting, deterministic, total
- 1-parameter: linear, nondeleting

Relation to tree transducers

Illustration



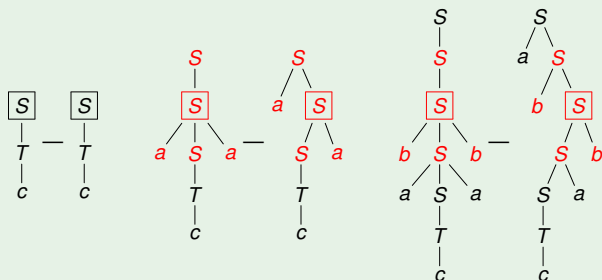
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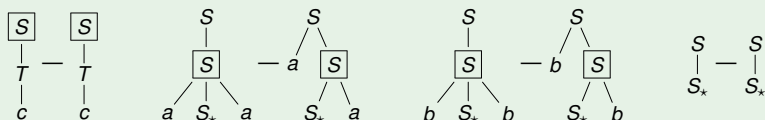
- linear, nondeleting, deterministic, total
- 1-parameter: linear, nondeleting

Copying example

Example

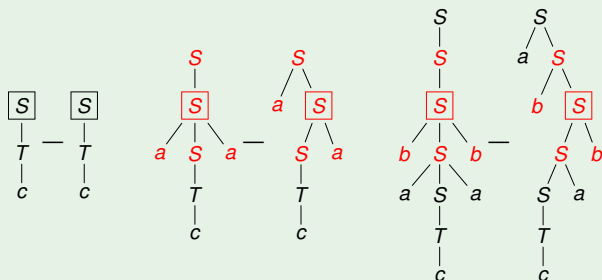


Example



Copying example

Example



String translation

$$\{(wcw^R, wcw) \mid w \in \{a, b\}^*\}$$

Basic properties

Example (Copying translation)

$$\tau_G = \{(wcw^R, wcw) \mid w \in \{a, b\}^*\}$$

Consequences

- STAG are *symmetric*
- STAG do not preserve regularity (neither direction)

Basic properties

Example (Copying translation)

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Consequences

- STAG are **symmetric**
- STAG do not preserve regularity (neither direction)

Summary

Model \ Criterion	EXPR	SYM	PRES	$PRES^{-1}$	COMP
Linear nondeleting TOP	X	X	✓	✓	✓
Linear nondeleting XTOP	✓	✓	✓	✓	X
Linear nondeleting XMBOT	✓	X	X	✓	✓
Linear XMBOT	✓	X	X	✓	✓
General XMBOT	✓	X	X	✓	X
reg.-preserving linear XMBOT	✓	X	✓	✓	✓
invertable linear XMBOT	✓	✓	✓	✓	✓
STAG	✓	✓	X	X	X

Implementation

XTAG [THE XTAG PROJECT 2008]

- Implements TAG, STAG
- Optimized for natural language applications
- Application of STAG

<http://www.cis.upenn.edu/~xtag/>

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References

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